

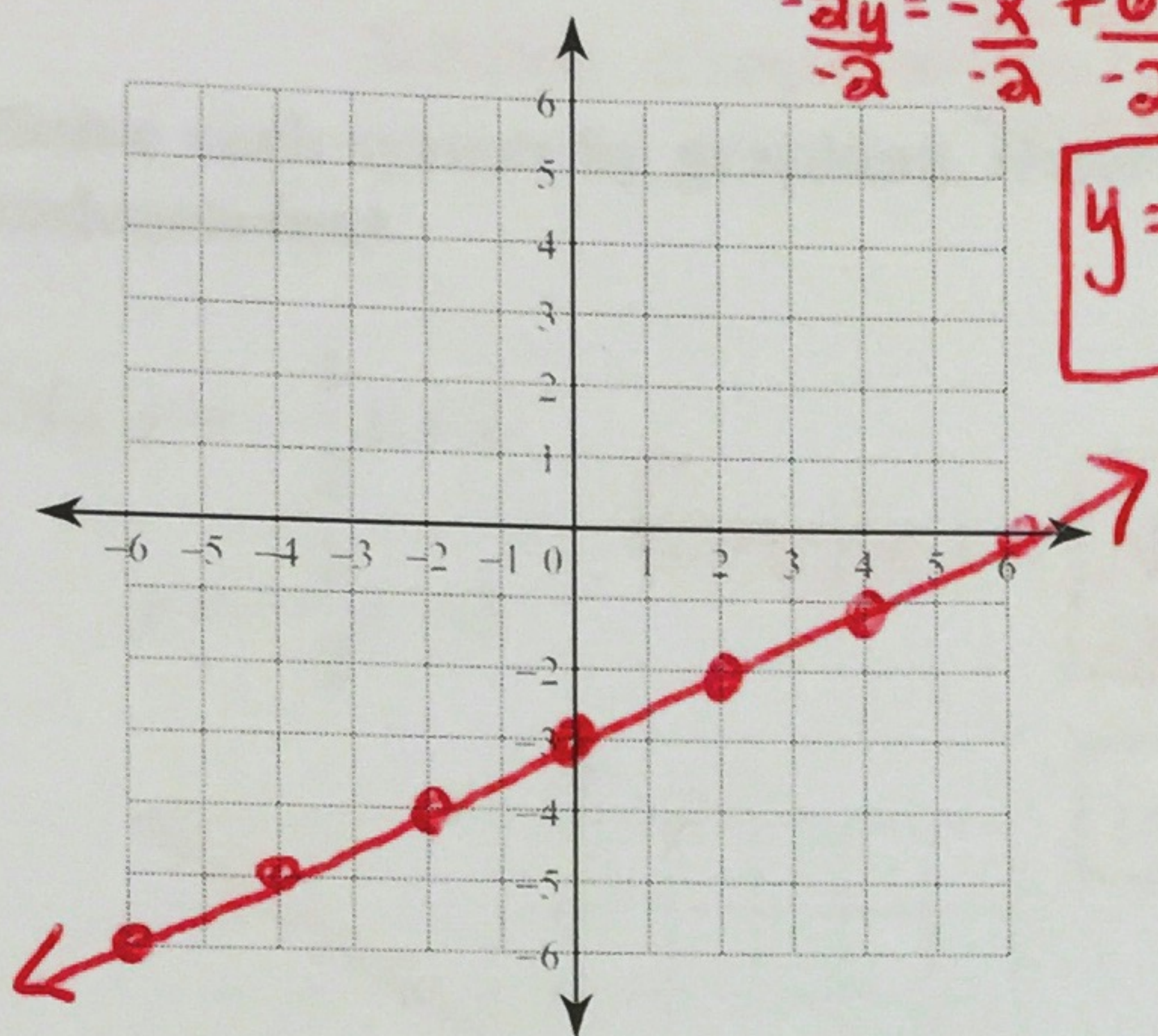
Study Guide--Systems of Linear Equations and Inequalities

Sketch the graph of each line.

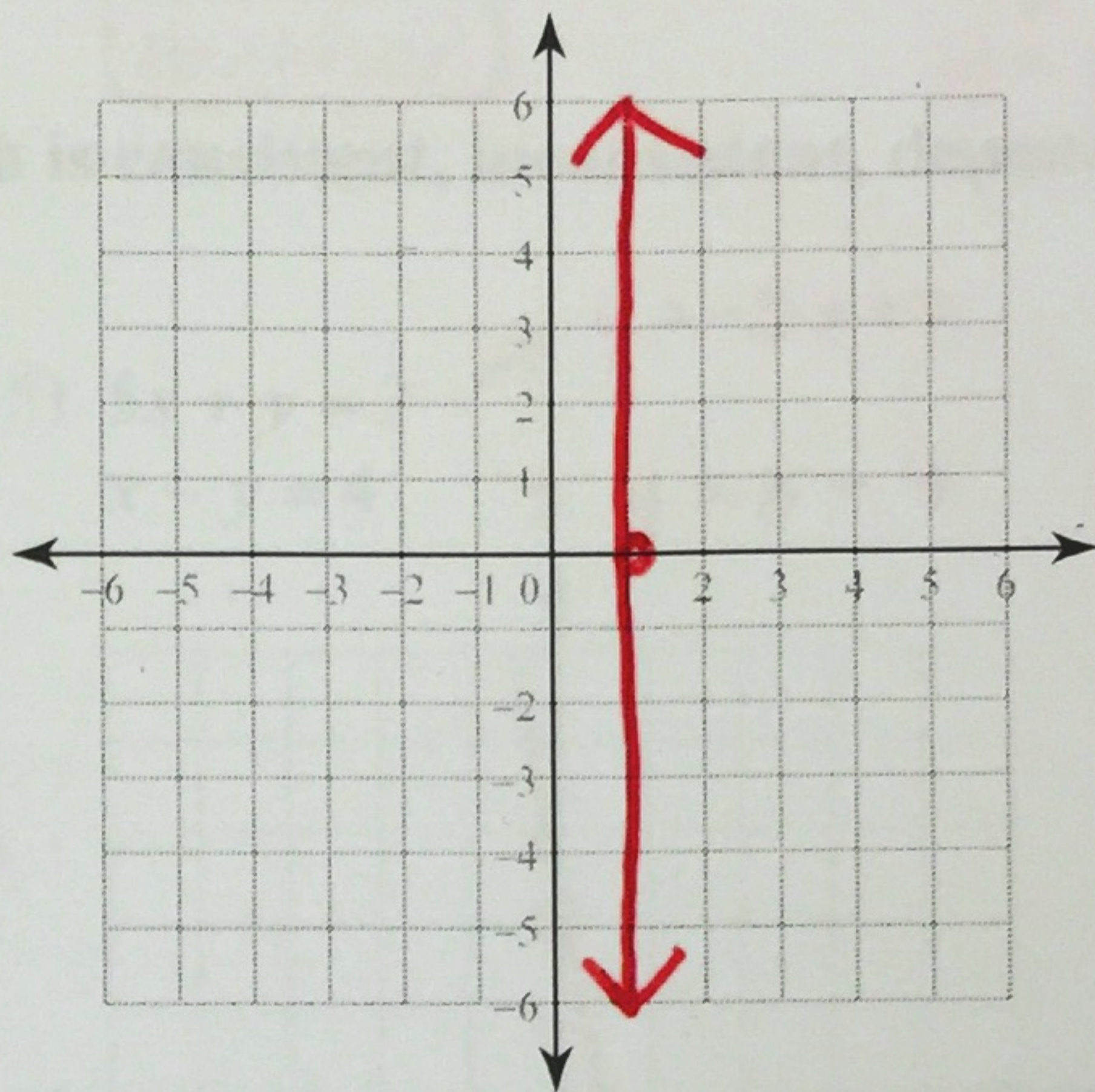
1) $x - 2y = 6$

$$\begin{aligned} x - 2y &= 6 \\ -x & \quad -x \\ \hline -2y &= -x + 6 \\ \frac{-2y}{-2} &= \frac{-x}{-2} + \frac{6}{-2} \end{aligned}$$

$$y = \frac{1}{2}x - 3$$



2) $x = 1$



Find the slope of each line.

3) $y = 5$

$$\text{slope} = 0$$

4) $6x - 5y = 5$

$$\begin{aligned} -6x & \quad -6x \\ \hline -5y &= -6x + 5 \\ \frac{-5y}{-5} &= \frac{-6x}{-5} + \frac{5}{-5} \end{aligned}$$

$$\text{slope} = \frac{6}{5}$$

$$y = \frac{6}{5}x - 1$$

Find the slope of the line through each pair of points.

5) $(-19, -9), (8, 5)$

$$\frac{5 - (-9)}{8 - (-19)} = \frac{14}{27}$$

6) $(9, -19), (9, 8)$

$$\frac{8 - (-19)}{9 - 9} = \frac{27}{0}$$

zero in denominator means slope is **undefined**

Write the slope-intercept form of the equation of the line described.

7) Slope = $\frac{7}{5}$, y-intercept = -2

$$y = \frac{7}{5}x - 2$$

8) through: $(-2, 1)$, slope = $\frac{1}{2}$

$$\begin{aligned} y &= mx + b \\ 1 &= \frac{1}{2}(-2) + b \\ 1 &= -1 + b \\ 2 &= b \end{aligned}$$

$$y = \frac{1}{2}x + 2$$

9) through: $(3, -2)$ and $(2, 3)$

① m
 $\frac{-2 - 3}{3 - 2} = \frac{-5}{1} = -5$

② b
 $-2 = -5(3) + b$
 $-2 = -15 + b$
 $13 = b$

$$y = -5x + 13$$

10) through: $(3, -3)$, parallel to $y = \frac{2}{3}x + 4$

$$-3 = \frac{2}{3}(3) + b$$

$$-3 = 2 + b$$

$$-5 = b$$

$$y = \frac{2}{3}x - 5$$

parallel \rightarrow same slope

11) through: $(2, -5)$, perp. to $y = \frac{2}{9}x - 1$

$$-5 = -\frac{9}{2}(2) + b$$

$$-5 = -9 + b$$

$$4 = b$$

$$y = -\frac{9}{2}x + 4$$

perp \rightarrow opp. sign reciprocal slope

check slopes!

Decide if each pair of lines is parallel, perpendicular, or neither. Your work should support your answers.

12) $-4x + 2y = 6$
 $-2x + y = -1$

$-4x + 2y = 6$
 $2y = 4x + 6$
 $y = 2x + 3$

$-2x + y = -1$
 $y = 2x - 1$

Same slope \rightarrow **parallel**

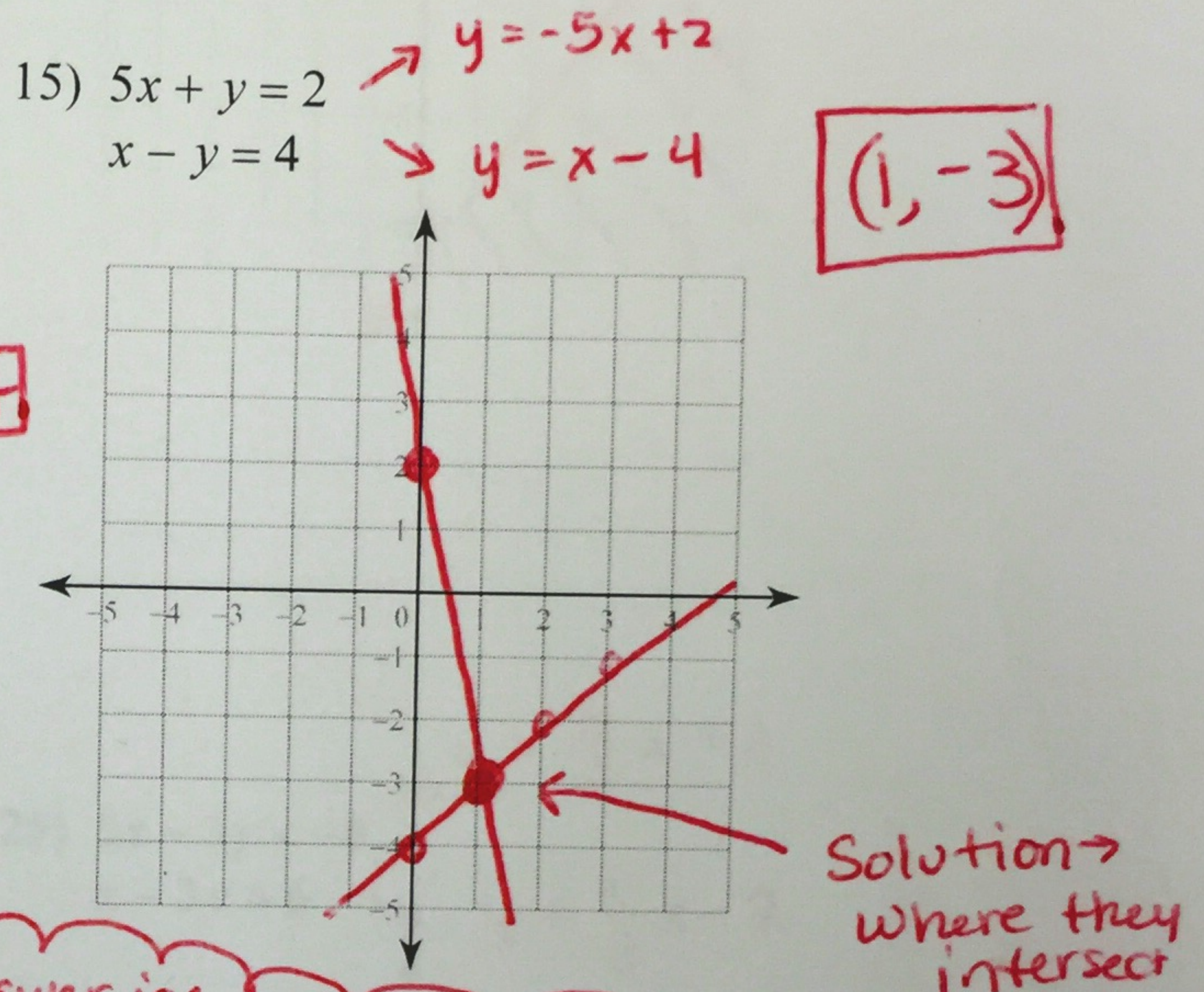
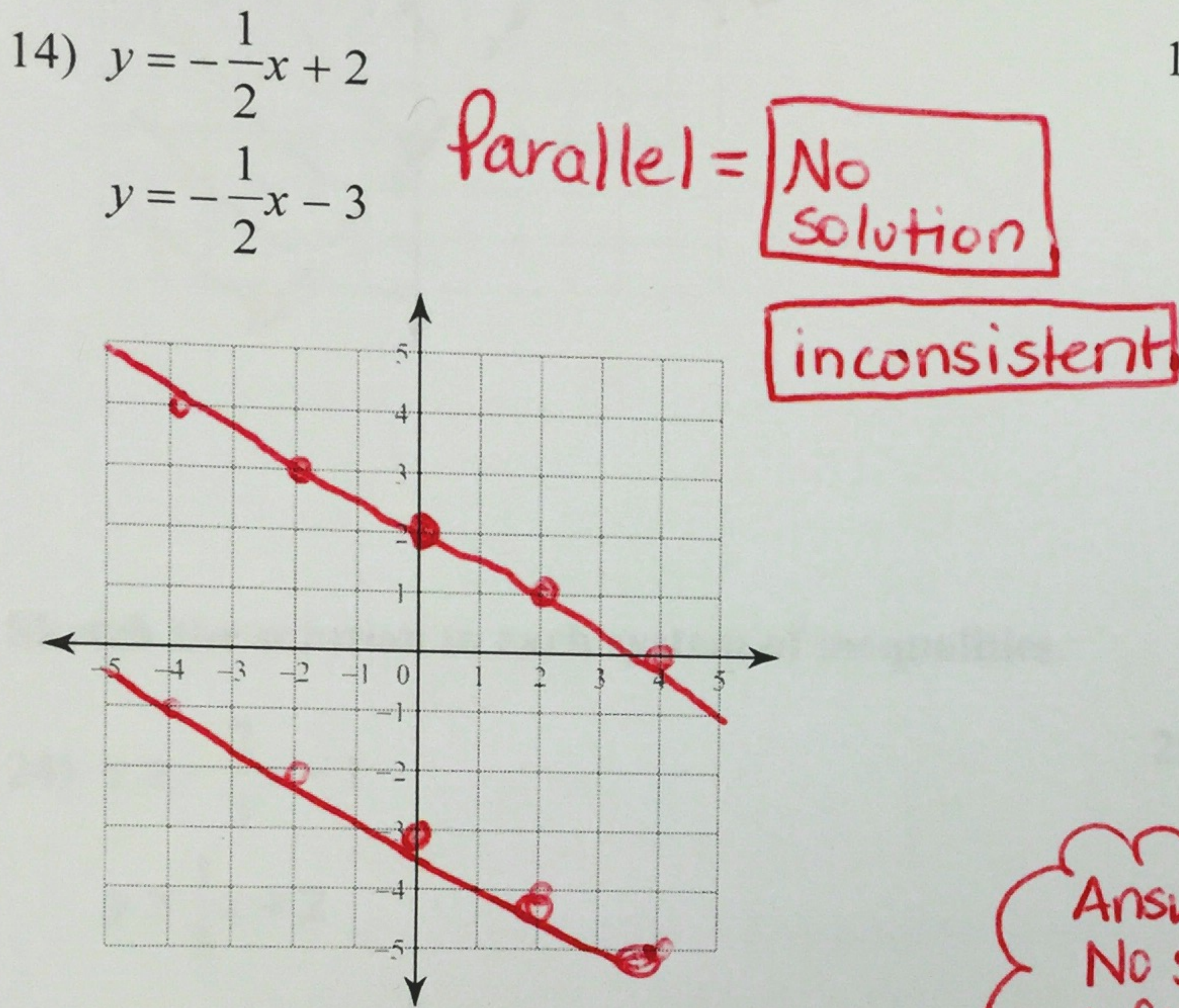
13) $12x + 2y = -14$
 $-12x + 2y = 4$

$12x + 2y = -14$
 $2y = -12x - 14$
 $y = -6x - 7$

$-12x + 2y = 4$
 $\frac{2y}{2} = \frac{12x + 4}{2}$
 $y = 6x + 2$

neither

Solve each system by graphing. Determine if the graph is consistent, inconsistent, or independent.



Answer is:
 No solution \rightarrow inconsistent
 Infinite solution \rightarrow dependent, consistent
 One solution \rightarrow independent, consistent

Solve each system by substitution. Answer

16) $7x + y = -15$
 $4x + 3y = -11$

$y = -7x - 15$ **(-2, 1)**

$4x + 3(-7x - 15) = -11$
 $4x - 21x - 45 = -11$
 $-17x = 34$
 $x = -2$

$7x + y = -15$
 $7(-2) + y = -15$
 $-14 + y = -15$
 $y = -1$

17) $-7x - 4y = -3$
 $x + 2y = -1$

$x = -2y - 1$

$-7(-2y - 1) - 4y = -3$
 $14y + 7 - 4y = -3$
 $10y = -10$
 $y = -1$

$x + 2(-1) = -1$
 $x - 2 = -1$
 $x = 1$

Answer (1, -1)

Solve each system by elimination.

18) $18x + 4y = -14$
 $2(-9x - 6y = 3)$

$18x + 4y = -14$
 $-18x - 12y = 6$
 $-8y = -8$
 $y = 1$

$18x + 4(1) = -14$
 $18x = -18$
 $x = -1$

(-1, 1)

19) $-14x + 8y = 0$
 $-2(-7x + 4y = 0)$

$-14x + 8y = 0$
 $14x - 8y = 0$

everything cancels

Infinite Solution

Solve the system using the method you prefer.

20) $-4x - 8y = -20$
 $-8x - y = -25$

$-8x - (1) = -25$
 $-8x = -24$
 $x = 3$

$8x + 16y = 40$
 $15y = 15$
 $y = 1$

(3, 1)

21) $x + 4y = 5$
 $-2x + 3y = 1$

$x = -4y + 5$
 $-2(-4y + 5) + 3y = 1$
 $8y - 10 + 3y = 1$
 $11y = 11$
 $y = 1$

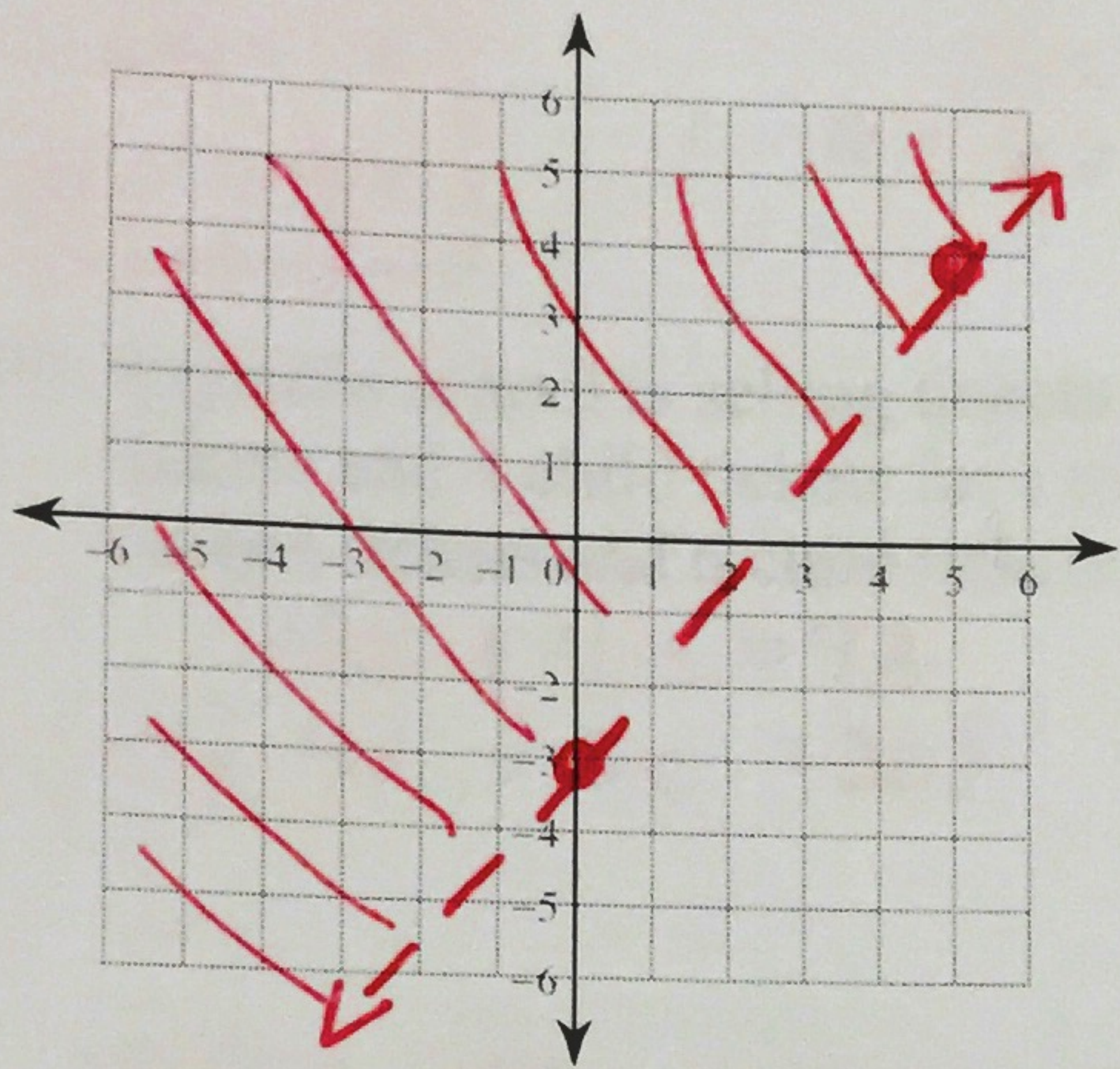
$x = -4(1) + 5$
 $x = 1$

(1, 1)

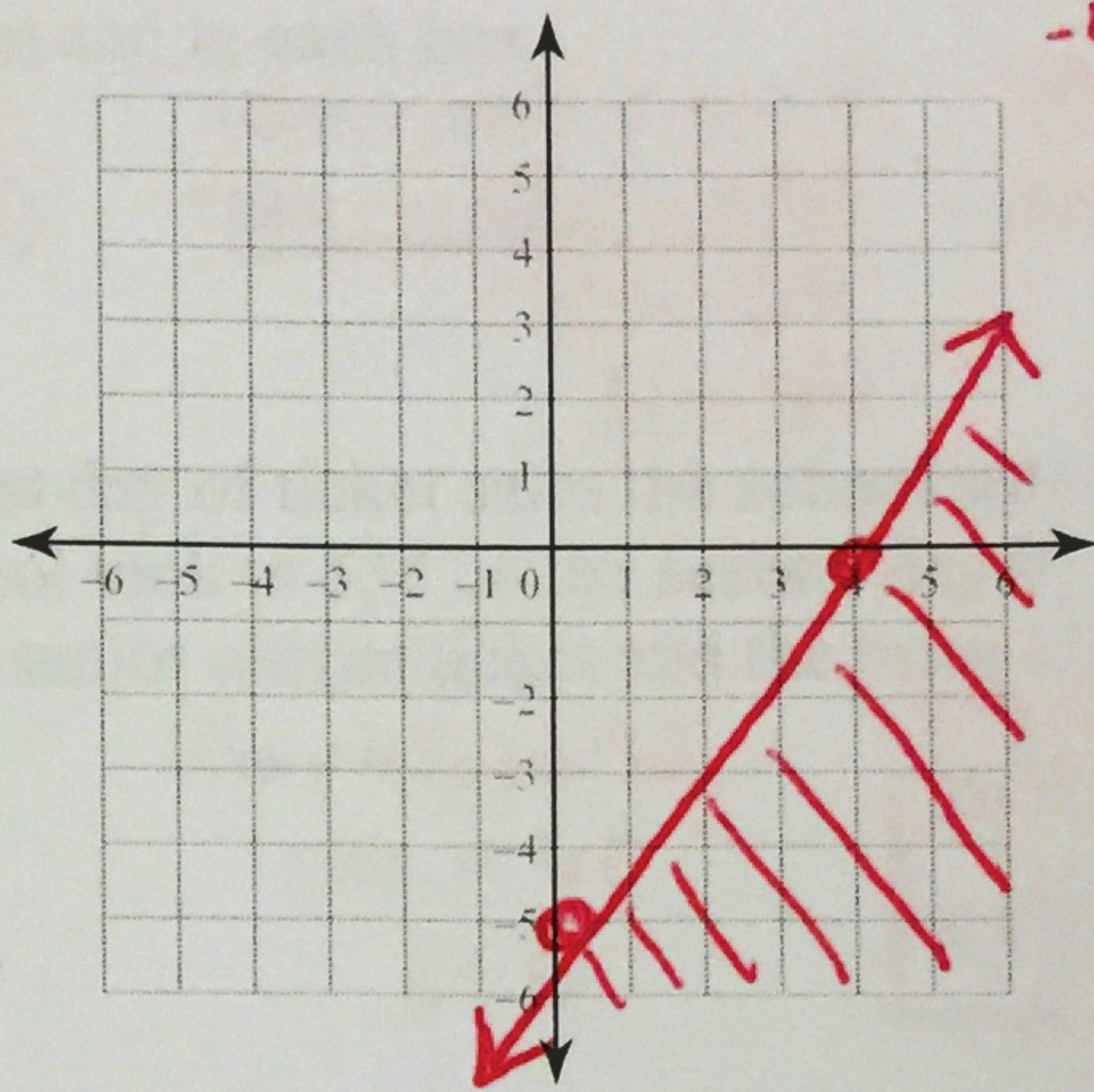
Sketch the graph of each linear inequality.

Shade above $>, \geq$ line dotted $>, <$
 below $<, \leq$ solid \geq, \leq

22) $y > \frac{7}{5}x - 3$



23) $5x - 4y \geq 20$

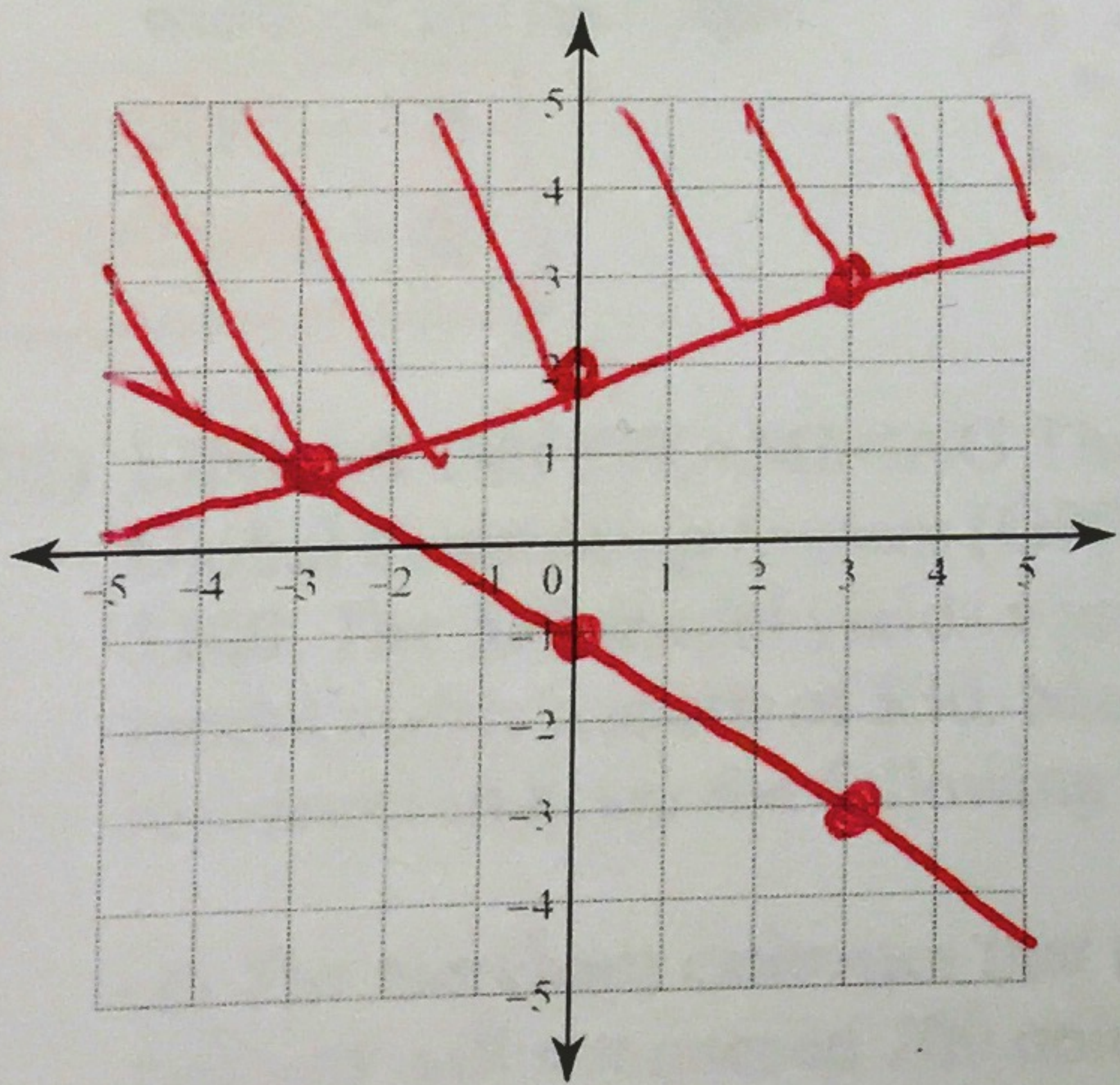


$-4y \geq -5x + 20$
 $y \leq \frac{5}{4}x - 5$

Sketch the solution to each system of inequalities.

24) $y \geq -\frac{2}{3}x - 1$

$y \geq \frac{1}{3}x + 2$

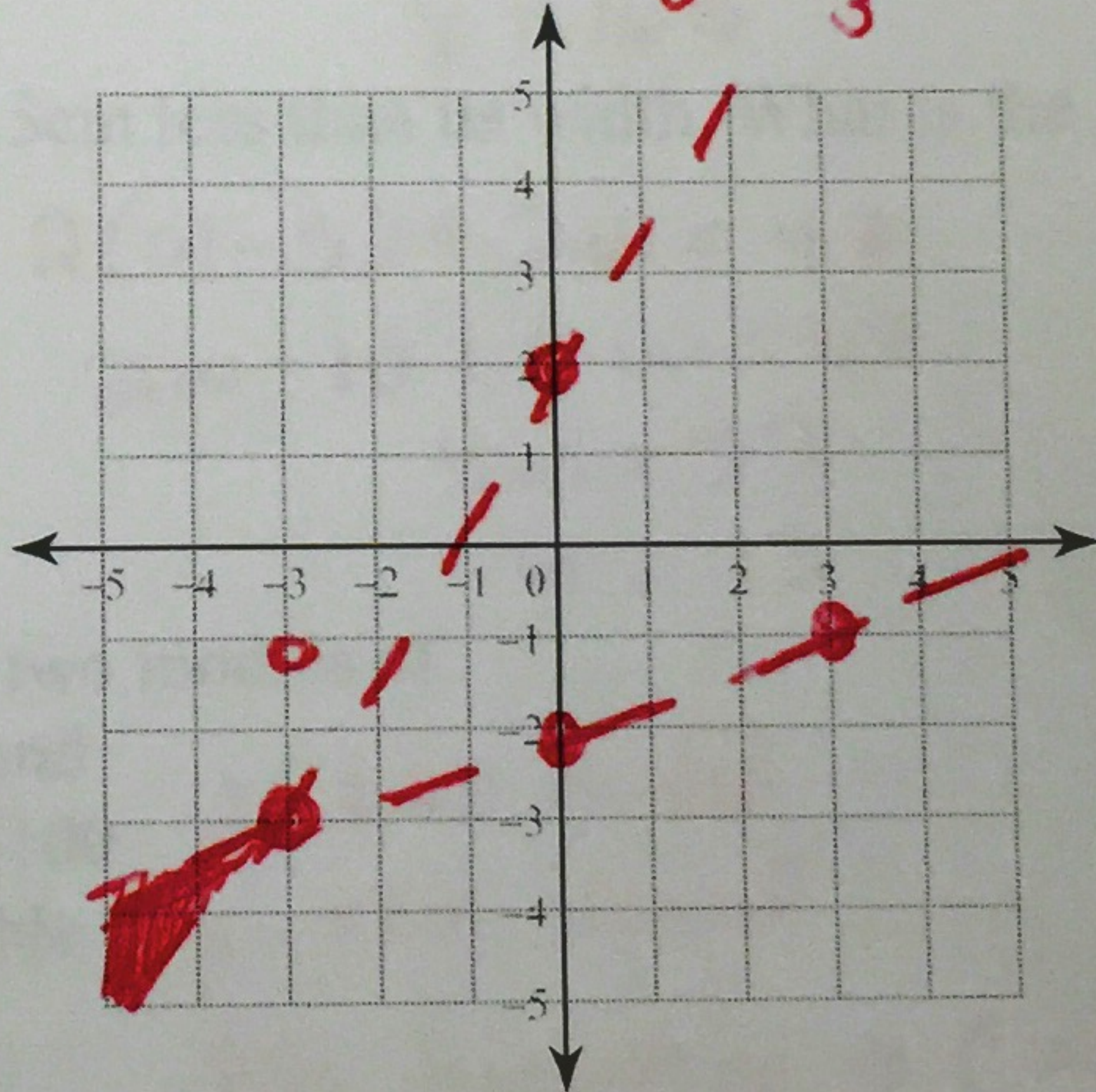


25) $5x - 3y < -6$

$x - 3y > 6$

$y > \frac{5}{3}x + 2$

$y < \frac{1}{3}x - 2$



26) A plane traveled 700 miles to Havana and back. The trip there was with the wind. It took 7 hours. The trip back was into the wind. The trip back took 14 hours. Find the speed of the plane in still air and the speed of the wind.

$700 \rightarrow 7 \text{ hrs} \rightarrow 100 \text{ mph}$

$14 \text{ hrs} \rightarrow 50 \text{ mph}$

$x + y = 100$

$x - y = 50$

$2x = 150$

$x = 75$

$75 + y = 100$

$y = 25$

plane - 75 mph

wind - 25 mph

- 27) The senior classes at High School A and High School B planned separate trips to the indoor climbing gym. The senior class at High School A rented and filled 12 vans and 13 buses with 634 students. High School B rented and filled 6 vans and 7 buses with 334 students. Every van had the same number of students in it as did the buses. Find the number of students in each van and in each bus.

$$\begin{aligned} \text{van} &= 16 \\ \text{bus} &= 34 \end{aligned}$$

$$\begin{aligned} 12v + 13b &= 634 \\ -2(6v + 7b &= 334) \end{aligned}$$

$$\begin{aligned} 12v + 13b &= 634 \\ -12v - 14b &= -668 \\ \hline -b &= -34 \\ b &= 34 \end{aligned}$$

$$\begin{aligned} 12v + 13(34) &= 634 \\ 12v + 442 &= 634 \\ 12v &= 192 \\ v &= 16 \end{aligned}$$

- 28) Krystal's school is selling tickets to a play. On the first day of ticket sales the school sold 12 senior citizen tickets and 4 child tickets for a total of \$72. The school took in \$38 on the second day by selling 4 senior citizen tickets and 6 child tickets. Find the price of a senior citizen ticket and the price of a child ticket.

$$\begin{aligned} 12s + 4c &= 72 \\ -3(4s + 6c &= 38) \end{aligned}$$

$$\begin{aligned} 12s + 4c &= 72 \\ -12s - 18c &= 114 \\ \hline -14c &= -42 \\ c &= 3 \end{aligned}$$

$$\begin{aligned} 12s + 4(3) &= 72 \\ 12s &= 60 \\ s &= 5 \end{aligned}$$

$$\begin{aligned} \text{Senior} &- \$5 \\ \text{child} &- \$3 \end{aligned}$$

Write a system of linear inequalities.

- 29) Hillary needs markers and poster board for a project. The markers are \$0.79 each and the poster board is \$1.89 per sheet. She needs at least 4 sheets of poster board. Hillary has \$15 to spend on project materials.

x - markers
y - poster board

$$\begin{aligned} 0.79x + 1.89y &\leq 15 \\ y &\geq 4 \end{aligned}$$

$$\begin{aligned} x &= 165 \\ y &= 49 \end{aligned}$$

- 30) The sum of two numbers is 214. The first number is 18 more than three times the second number. What are the two numbers?

$$x + y = 214$$

$$18 + 3y + y = 214$$

$$x = 18 + 3y$$

$$4y = 196$$

$$x = 18 + 3(49)$$

$$y = 49$$

$$x = 165$$

- 31) A rectangle has a perimeter of 42cm and its length is 5cm less than its width. What is the length and width of the rectangle?

$$\begin{aligned} \text{width} &- 13 \\ \text{length} &- 8 \end{aligned}$$

$$\begin{aligned} 2l + 2w &= 42 \\ l &= w - 5 \end{aligned}$$

$$2(w - 5) + 2w = 42$$

$$l = w - 5$$

$$2w - 10 + 2w = 42$$

$$l = 13 - 5$$

$$4w = 52$$

$$l = 8$$

$$w = 13$$

- 32) LINEAR PROGRAMMING The costs to a store for two models of Global Positioning System (GPS) receivers are \$80 and \$100. The \$80 model yields a profit of \$25 and the \$100 model yields a profit of \$30. Market tests and available resources indicate the following constraints.

x - \$80 model

y - \$100 model

$$\text{Obj. function} \rightarrow C = 25x + 30y$$

- (a) The merchant estimates that the total monthly demand will not exceed 200 units.

$$x + y \leq 200$$

- (b) The merchant does not want to invest more than \$18,000 in GPS receiver inventory.

$$80x + 100y \leq 18000$$

this is your profit

What is the optimal inventory level for each model? 100 of each model
What is the optimal profit? \$5500.00

Draw a graph to find your feasible area.

Constraints

$$x + y \leq 200$$

$$80x + 100y \leq 18000$$

Obj Func. $25x + 30y$

$$(0,0) \rightarrow 25(0) + 30(0) = 0$$

$$(0,180) \rightarrow 25(0) + 30(180) = 5400$$

$$(200,0) \rightarrow 25(200) + 30(0) = 5000$$

$$(100,100) \rightarrow 25(100) + 30(100) = 5500$$

