

Benchmark 2--Study Guide

Name _____ Date _____ Period _____

Solve each equation.

1) $-3k - 4 = -8 - 5k$
 $15k - 4 + 4 = -8 - 5k + 4$
 $15k = -4$
 $k = -\frac{4}{15}$

2) $6 - 7x = -1 - 7x$
 $7x + 7x - 6 + 6 = -1 - 7x + 7x$
 $0 = -7$
 NS

Solve each inequality and graph its solution.

3) $-106 \leq -3(5x + 5) + 2x$

$\leq \geq$ closed
 $< >$ open

$-106 \leq -15x - 15 + 2x$
 $-106 \leq -13x - 15$
 $-91 \leq -13x$
 $7 \geq x$
 $x \leq 7$
 be sure to turn it around

Sketch the graph of each linear inequality.

4) $-6 + 3b \geq 21$ or $9 + 7b \leq -47$

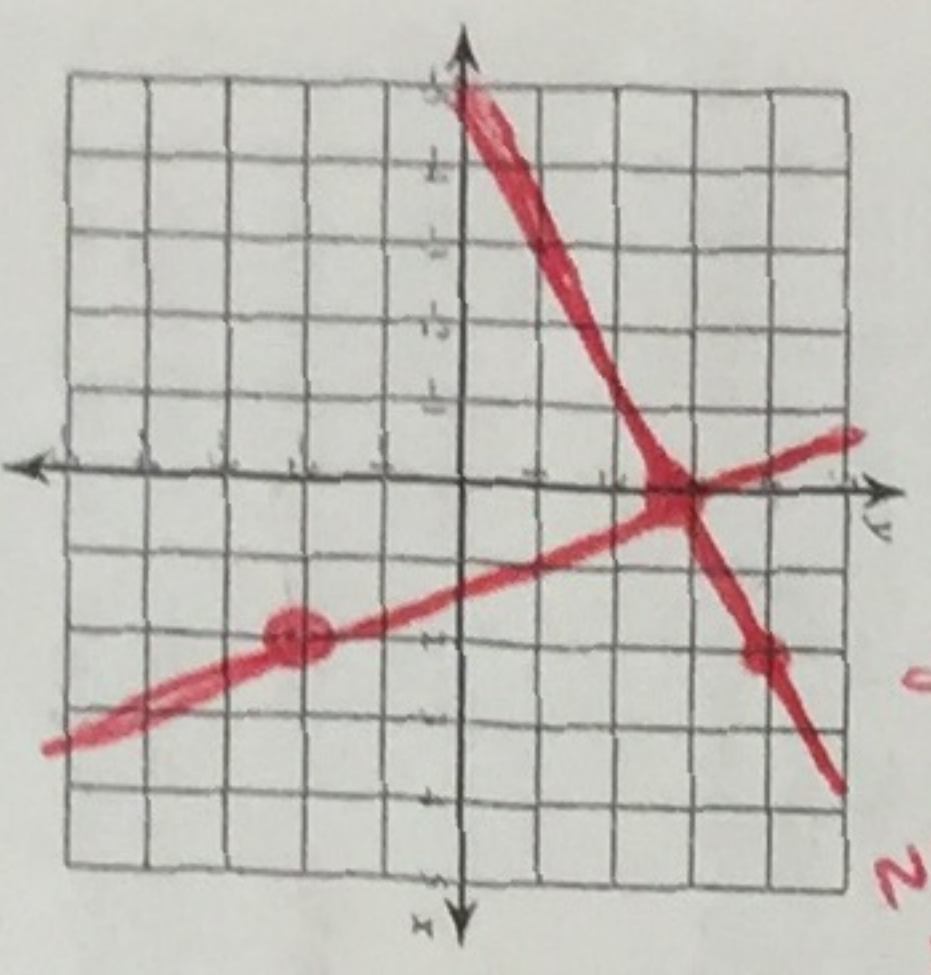
$-6 + 3b \geq 21$
 $3b \geq 27$
 $b \geq 9$
 $9 + 7b \leq -47$
 $7b \leq -56$
 $b \leq -8$

5) $6m + 5 > -49$ and $-7m - 3 > -73$

$6m + 5 > -49$
 $6m > -54$
 $m > -9$
 $-7m - 3 > -73$
 $-7m > -70$
 $m < 10$

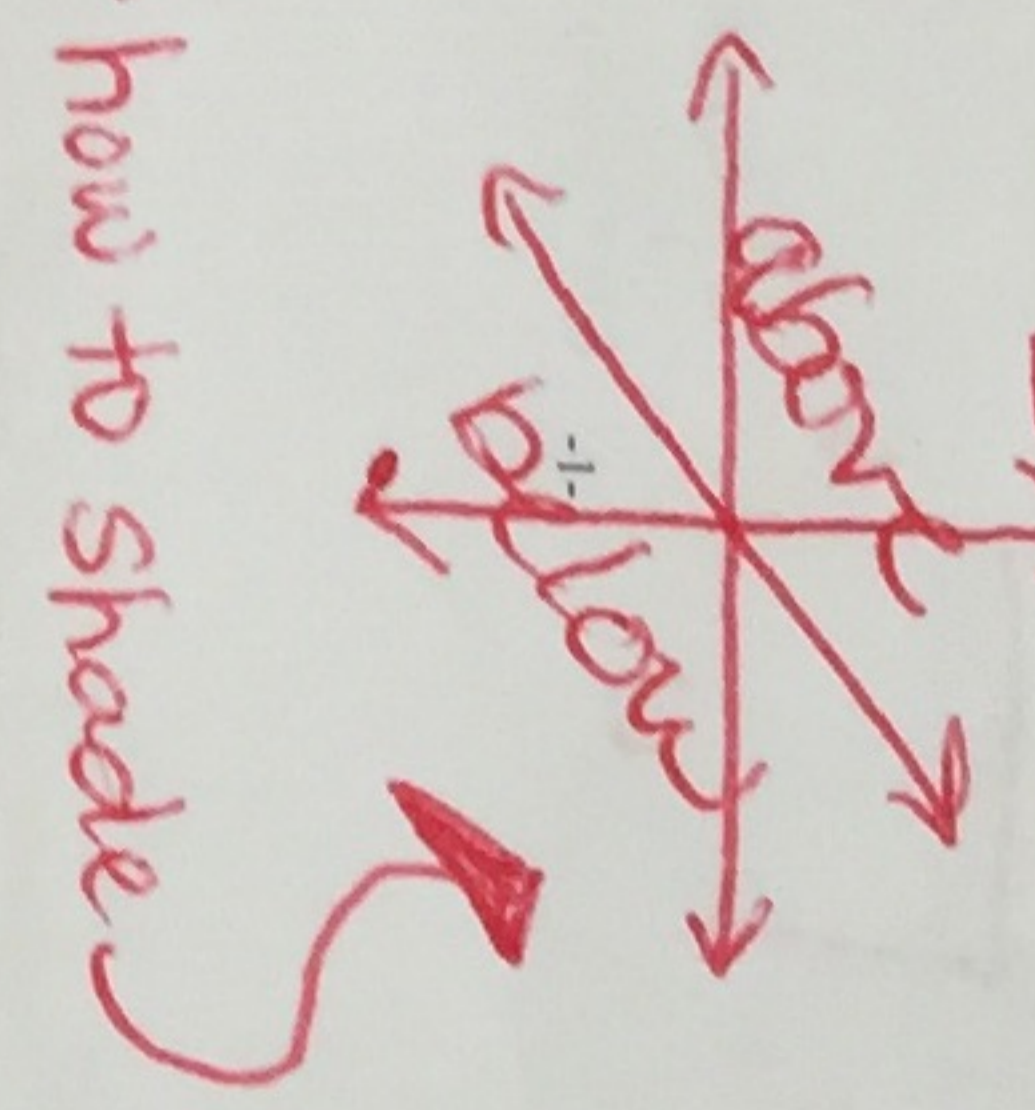
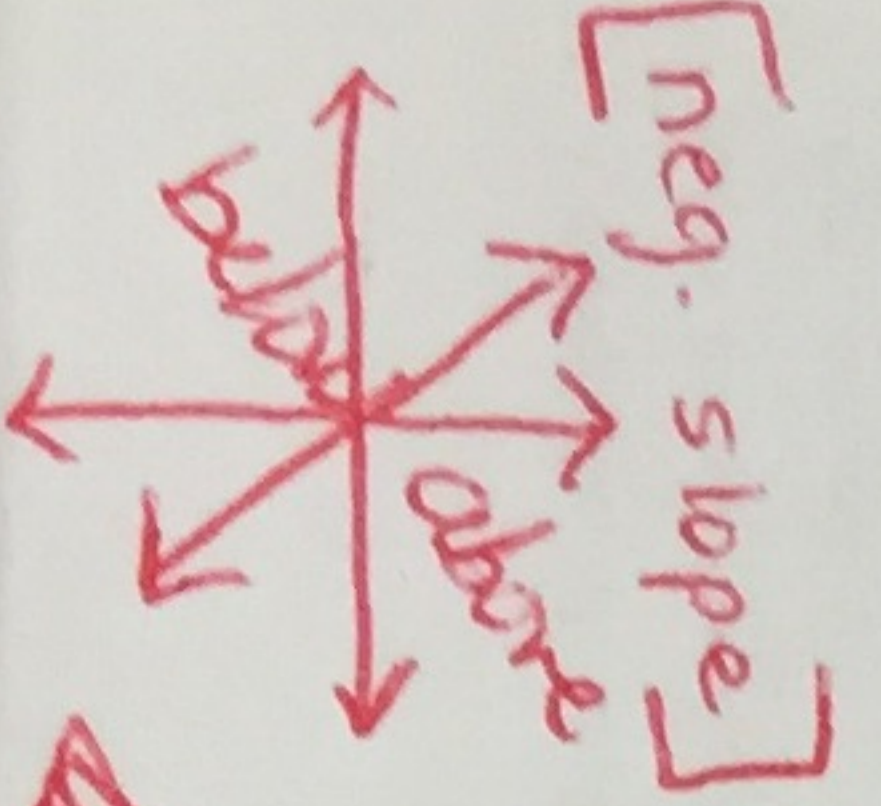
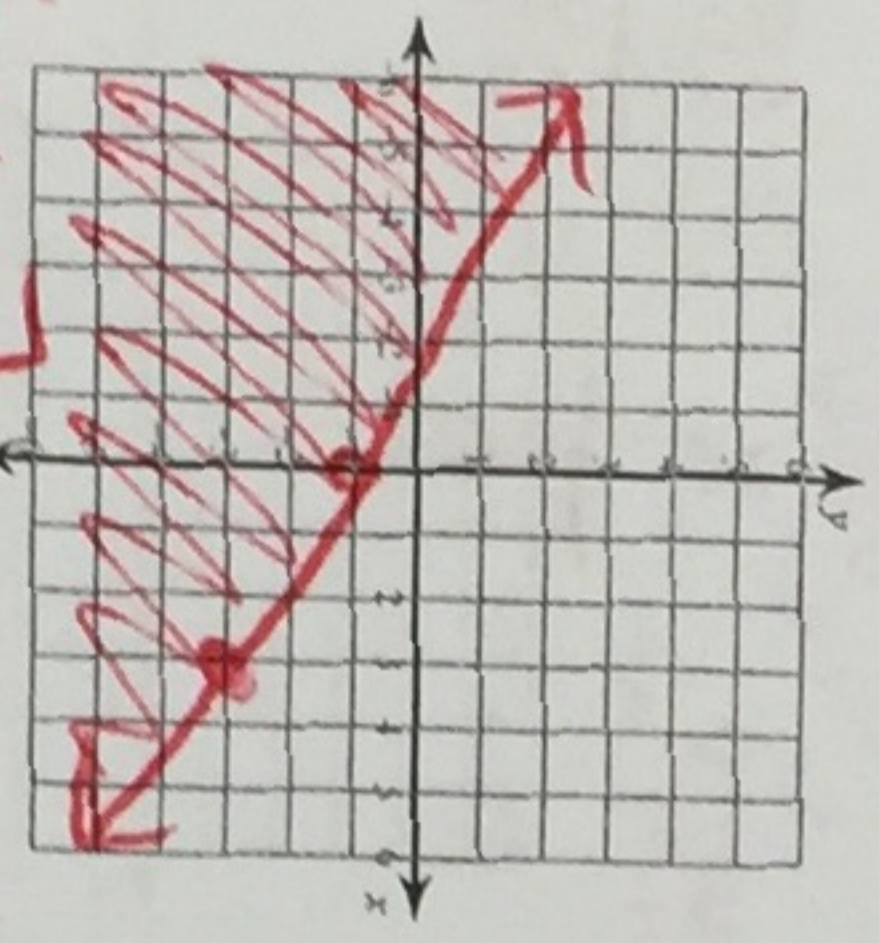
Solve each system by graphing.

6) $2y = -5x + 6$
 $-3 + \frac{1}{2}x = y$
 $y = -\frac{5}{2}x + 3$
 $y = \frac{1}{2}x + 3$



Solve each system by substitution.

7) $2x + 3y \leq -3$
 $3y \leq -2x - 3$
 $y \leq -\frac{2}{3}x - 1$



Shade above $> , \geq$
 below $< , \leq$
 Line dotted $> , <$
 solid \geq , \leq

Solve each system by substitution.

8) $-8x + y = -6$
 $-16x + 2y = -4$
 $y = 8x - 6$
 $-16x + 2(8x - 6) = -4$
 $-16x + 16x - 12 = -4$
 $-12 = -4$
 NS

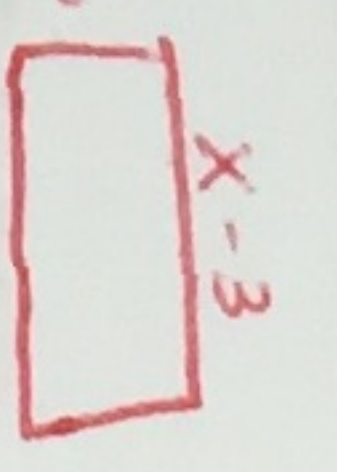
Solve each system by elimination.

9) $2x + 4y = 14$
 $9x + 8y = -7$
 $-4x - 8y = -28$
 $9x + 8y = -7$
 $5x = -35$
 $x = -7$
 $2(-7) + 4y = 14$
 $-14 + 4y = 14$
 $4y = 28$
 $y = 7$
 (-7, 7)

10) Jaidee and Amanda each improved their yards by planting hostas and geraniums. They bought their supplies from the same store. Jaidee spent \$63 on 7 hostas and 7 geraniums. Amanda spent \$102 on 14 hostas and 10 geraniums. What is the cost of one hosta and the cost of one geranium?

$7h + 7g = 63$
 $14h + 10g = 102$
 $-14h - 14g = -126$
 $14h + 10g = 102$
 $-4g = -24$
 $g = 6$
 $7h + 7(6) = 63$
 $7h + 42 = 63$
 $7h = 21$
 $h = 3$
 (6, 3)

11) A rectangle has a length of $x - 3$ inches and a width of 6 inches. For what values of x is the area of the rectangle greater than the perimeter of the rectangle? Draw a diagram to help.



$a > p$
 $6(x-3) > 2(x-3) + 2(6)$
 $6x - 18 > 2x - 6 + 12$
 $6x - 18 > 2x + 6$
 $4x > 24$
 $x > 6$
 $45m$ in 4 hrs = 11.25 miles
 $11.25m$ in 1 hr (miles)
 $59400 = 3600$ (secs in a hr)

13) Solve $\frac{m}{x} = k - 6$ for m .

$m = x(k - 6)$ or $m = xk - 6x$

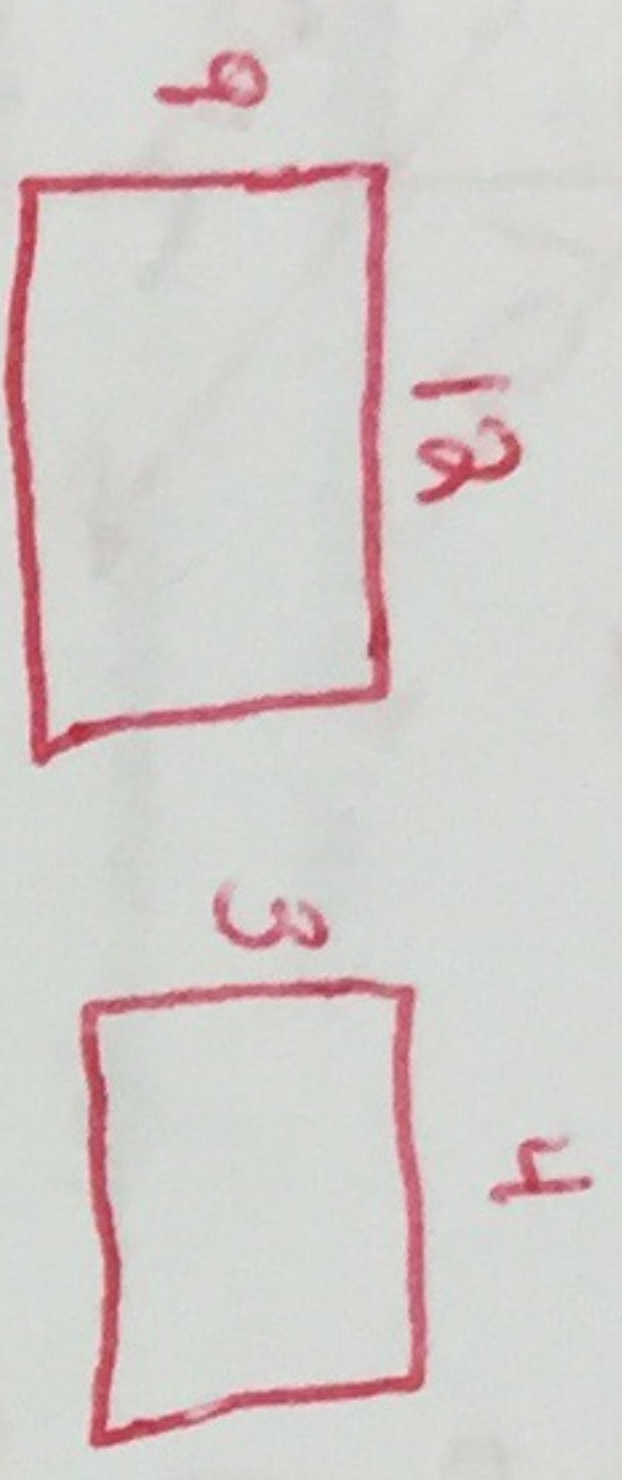
14) A weight that measures exactly 3,000 ounces is placed on three different balance scales. The results are below:

- Scale 1 : 3.03 ounces
- Scale 2 : 2.99 ounces
- Scale 3 : 3.014 ounces

Which scale is the most precise? 3
 Which scale is the most accurate? 2
 precise \rightarrow most decimal places
 accurate \rightarrow closest to a actual weight

15) A rectangle has side lengths of 12 inches and 9 inches. Every dimension is multiplied by $\frac{1}{3}$ to form a new rectangle.

What is the scale factor? $\frac{1}{3}$
 What is the ratio of the corresponding sides of the first figure to the second figure? $3:1$
 What is the ratio of the perimeters? $3:1$
 What is the ratio of the areas? $9:1$



16) An architect built a scale model of a shopping mall. On the model, a circular fountain is 20 inches tall and 22.5 inches in diameter. The actual fountain is to be 8 feet tall. What will be the diameter of the fountain?

$20 = \frac{8}{x}$ tall
 $22.5 = \frac{8}{x}$ diameter

$40x = 8 = 0.4$

$39.6 - 40.4$

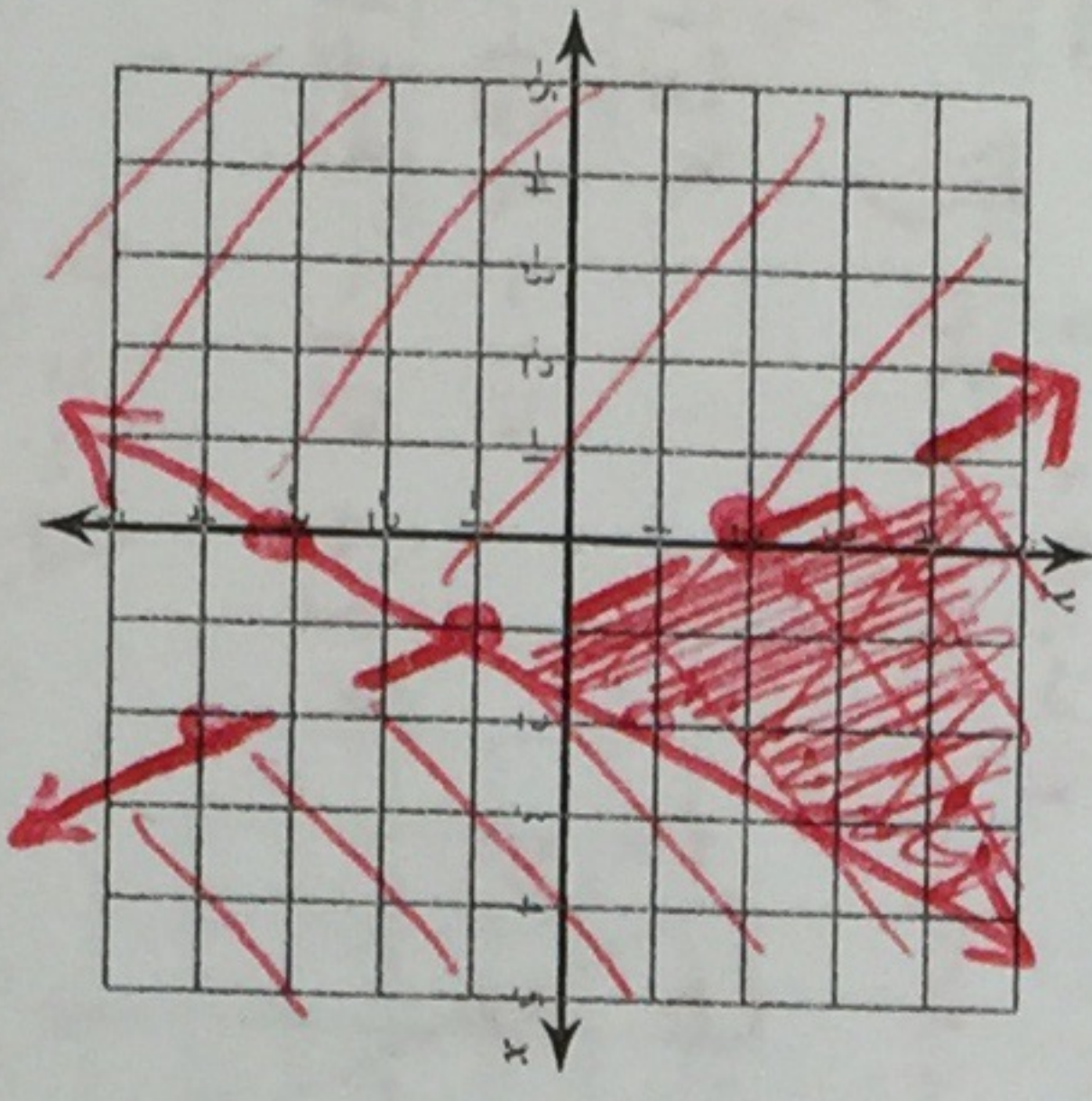
Solve each proportion.

18) $\frac{9}{7} = \frac{r+6}{10}$
 $90 = 7r + 42$
 $48 = 7r$

6.85

Sketch the solution to each system of inequalities.

19) $y \geq 2x - 3$
 $y > -3x + 2$



Double shaded region is the solution set

Write the slope-intercept form of the equation of the line through the given point with the given slope.

21) through: (3, -4), slope = $-\frac{7}{3}$
 $-4 = -\frac{7}{3}(3) + b$
 $-4 = -7 + b$
 $3 = b$

$y = -\frac{7}{3}x + 3$

Write the slope-intercept form of the equation of the line described.

23) through: (-4, -1), parallel to $y = \frac{3}{2}x + 1$
 $-1 = \frac{3}{2}(-4) + b$
 $-1 = -6 + b$
 $5 = b$

$y = \frac{3}{2}x + 5$

Find the slope of the line through each pair of points:

25) (8, -11), (-2, 11)
 $\frac{-11 - 11}{8 - (-2)} = \frac{-22}{10} = -\frac{11}{5}$

$-\frac{11}{5}$

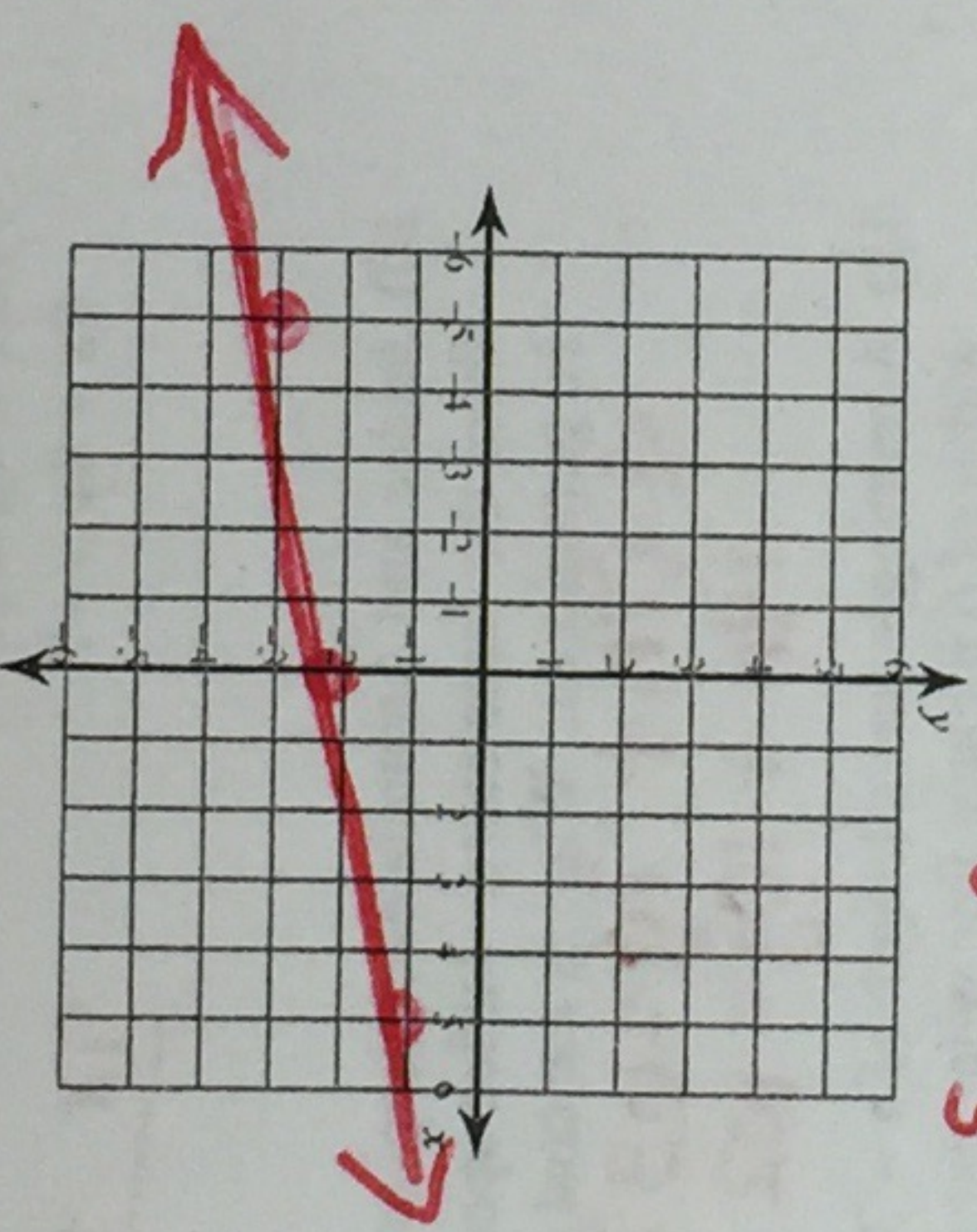
Find the x-intercept and the y-intercept.

27) $x + 3y = -9$
 $x = -9$
 $3y = -9$
 $y = -3$

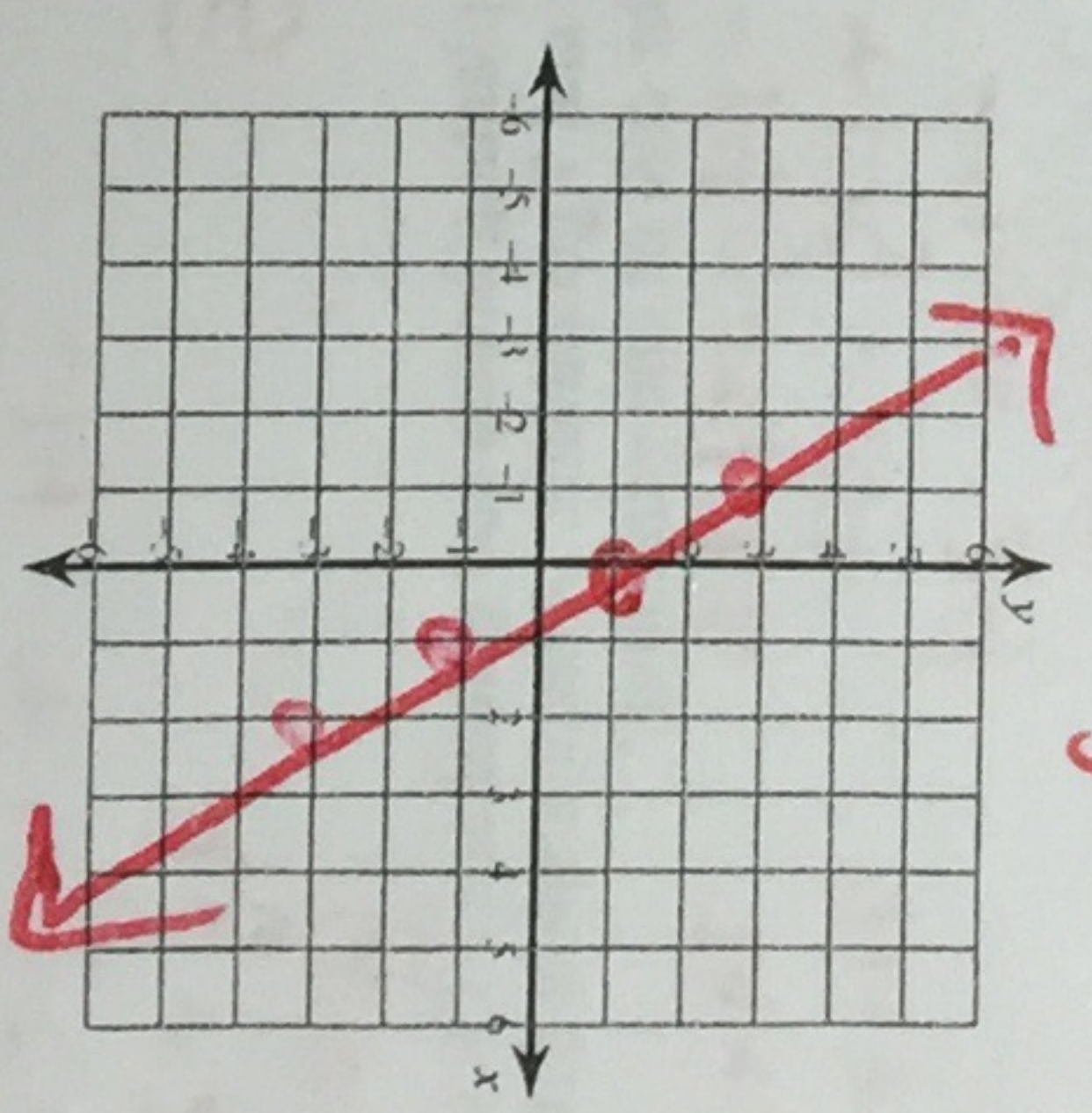
$x\text{-int} = -9$
 $y\text{-int} = -3$

Sketch the graph of each line. Then describe the transformations from the parent function $y = x$.

28) $x - 5y = 10$
 $y = \frac{1}{5}x - 2$



29) $2x + y = 1$
 $y = -2x + 1$



Write the slope-intercept form of the equation of the line through the given points.

22) through: (0, 3) and (4, -2)
 $\frac{3 - (-2)}{0 - 4} = \frac{5}{-4} = -\frac{5}{4}$

$y = -\frac{5}{4}x + 3$

$3 = -\frac{5}{4}(0) + b$
 $3 = b$

perp sign & opp recip unless perp to y = x

Write the slope-intercept form of the equation of each line given the slope and y-intercept.

20) Slope = -1, y-intercept = 3
 $m = -1$
 $b = 3$

$y = mx + b$

$y = -1x + 3$

$y = -x + 3$

Determine if the sequence is arithmetic. If it is, find the common difference, the 52nd term, and the explicit formula.

30) -6, -10, -14, -18, ...
 $a_n = a_1 + (n-1)d$
 $d = -4$

ef: $-6 - 4(n-1)$

$-2 - 4n$

$-2 - 4(52) = -210$

31) 28, 58, 88, 118, ...
 $d = 30$

ef: $28 + (n-1)30$

$28 + 30n - 30 = -2 + 30n$

$28 + 30(52) = 1558$

Determine if the sequence is geometric. If it is, find the common ratio, the 8th term, and the explicit formula.

32) 4, -8, 16, -32, ...

$r = -2$

33) 4, 16, 64, 256, ...

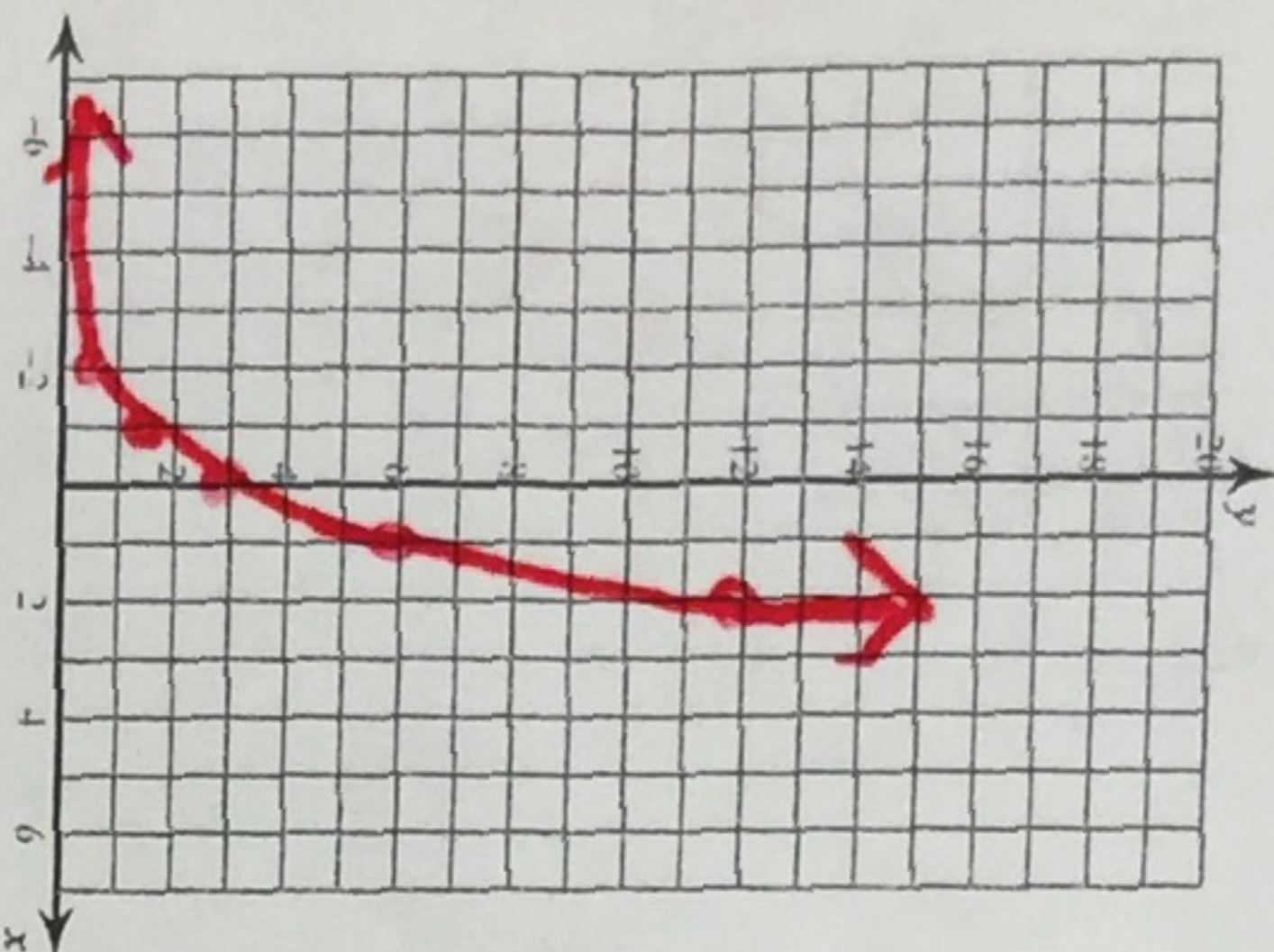
$R: 4$

EF: $4 \cdot (-2)^{n-1}$
 $8^{th}: 4 \cdot (-2)^7 = -512$

EF: $4 \cdot 4^{n-1}$
 $8^{th}: 4 \cdot 4^7 = 65536$

Sketch the graph of each function.

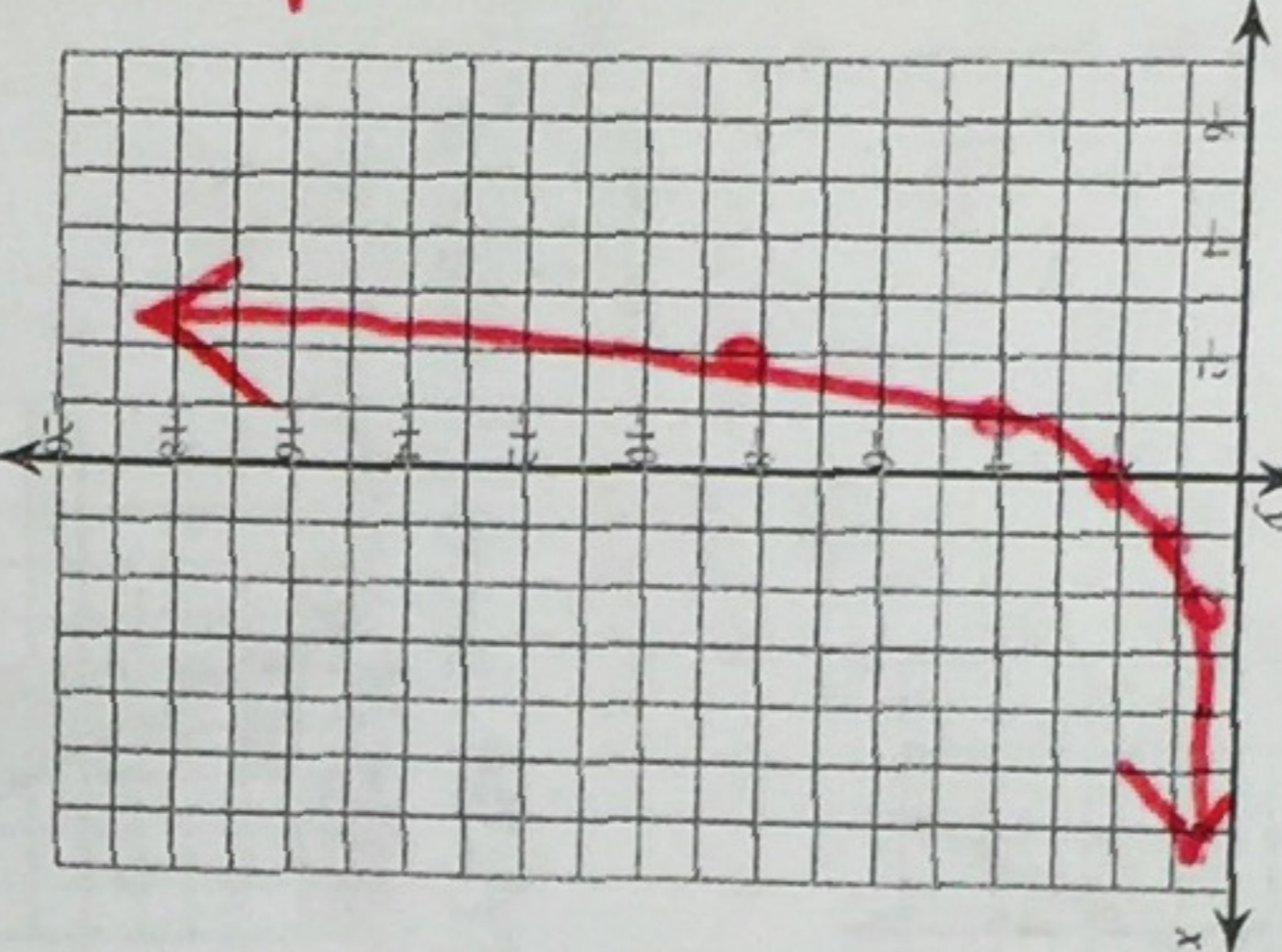
34) $y = 3 \cdot 2^x$



x	y
0	3
1	6
2	12

Use points -2 to 2

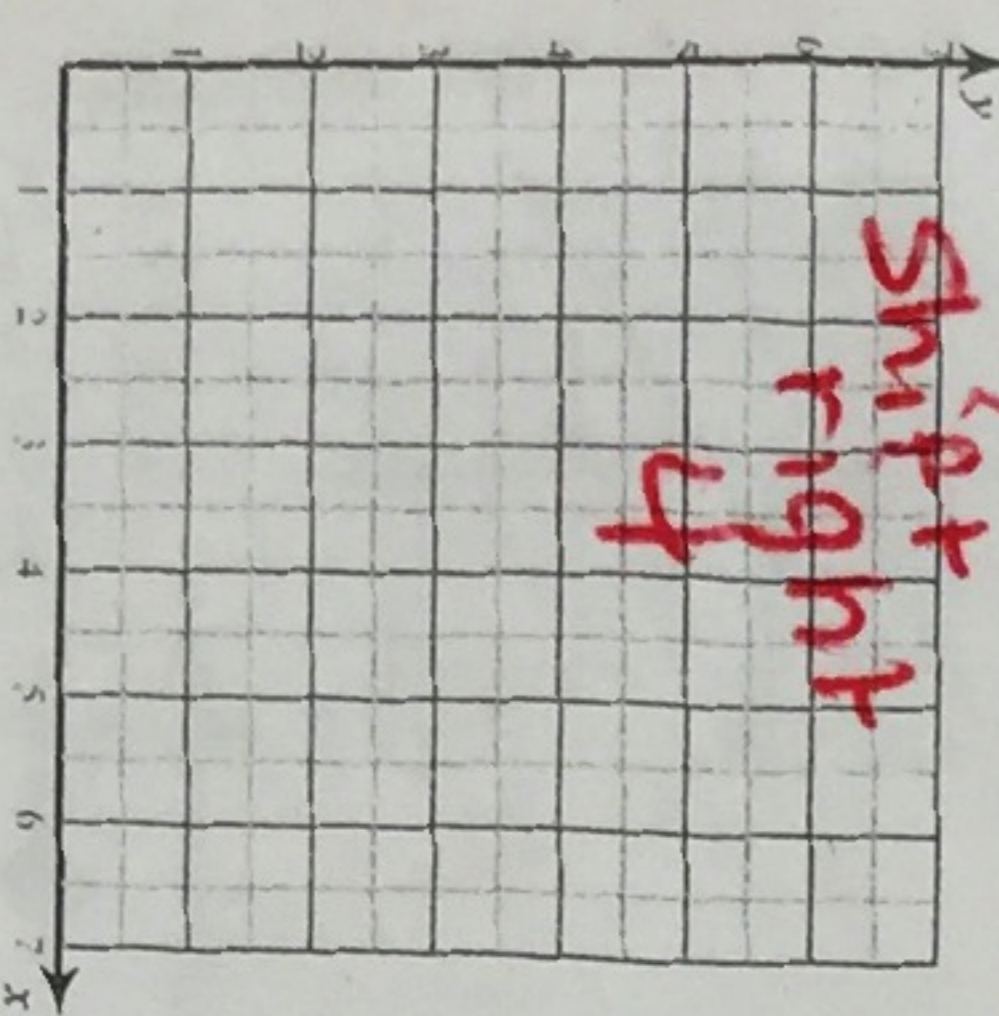
35) $y = -2 \cdot \left(\frac{1}{2}\right)^x$



x	y
0	-2
-1	-4
-2	-8

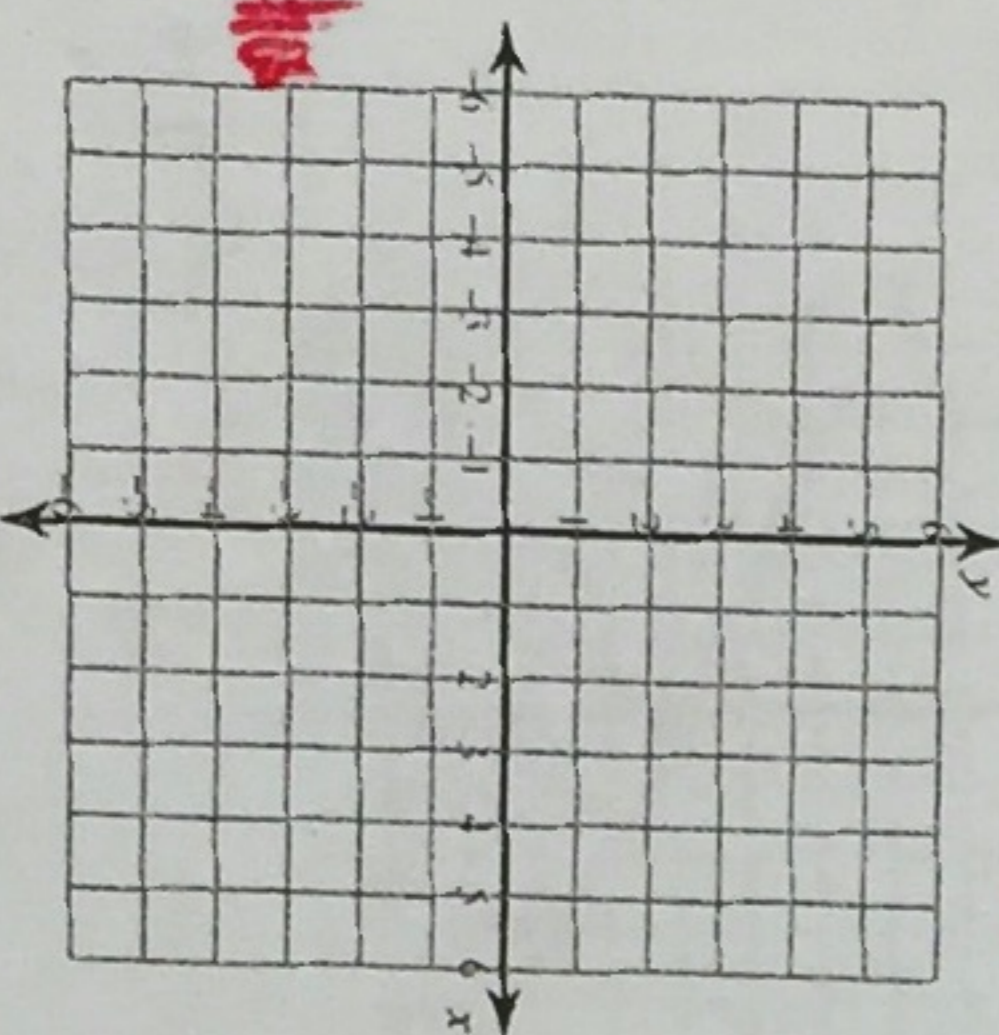
Analyze the graph of the following function:

36) $y = (x-4)^2 + 2$



Don't need to sketch - describe transform

37) $y = -|x-4| - 1$



reflect across x, shift right, shift down

Write an exponential model and find the total value of the investment after the time given.

38) \$57,000 at 3% compounded annually for 4 years

$57000 \left(1 + \frac{.03}{1}\right)^{4 \cdot 1}$

39) \$37,000 at 12.6% compounded quarterly for 2 years

$37000 \left(1 + \frac{.126}{4}\right)^{4 \cdot 2}$

40) Flourine-20 has a half-life of 11 seconds.

Find the amount of Flourine-20 left from a 40 gram sample after 2.2 minutes.

$40(.5)^{12} = 0.01$

41) The value of a gold coin is \$150 and is increasing at a rate of 15% each year. Find the value of the coin in 11 years.

$150(1 + .15)^{11} = 697.86$

Look for a pattern in each data set to determine which kind of model best describes the data.

42) $\{(0,6), (1, 12), (2, 24), (3, 48)\}$

$x \cdot 2 \rightarrow x \cdot 2 \rightarrow x \cdot 2$

Exponential

43) $\{(3, 4), (6, -2), (9, -8), (12, -14)\}$

$-6 - 6 - 6$

Linear

Compare the average rates of change over the interval given.

44) Michael is studying population changes in two types of birds living on an island. Compare the population by finding and interpreting the average rate of change over the interval (0, 18).

Time (months)	0	6	12	18
Pop. (thousands)	8.3	8.6	8.8	9.1

$\frac{8.3-9.1}{0-18} = \frac{-0.8}{-18} = .044 \approx 44$

≈ 44

Bird A

$y = 3.6 \cdot 1.06^x$

$(0, 3.6), (18, 10.2156)$

$\frac{3.6 \cdot 10.6 - 3.6 \cdot 1.06^0}{18 - 0} = \frac{3.6 \cdot 10.2156 - 3.6}{18} = \frac{36.776 - 3.6}{18} = \frac{33.176}{18} \approx 1.84$

Bird B is growing faster

45) Mr. Krabbs has \$2500 in his savings account. He wants to save more money. He is considering two plans. Under Plan 1 he will increase his balance by \$500 each year. Under Plan 2, he will increase his balance by 25% each year. How much more will he save with Plan 2 after 10 years? Round to the nearest hundredth.

Plan 1: $2500 + 500 \times 10 = 7500$

Plan 2: $2500(1 + .25)^{10} \approx 23283.06$