Algebra 1
Name $\qquad$
Systems of Equations Review
Date $\qquad$
3 Types of Special Systems Solutions

1) Infinite Solutions
2) No Solution

- all points in common
- Same equation
- no points in common
- same slopes
- Same line
- parallel lines

3) One Solution

- Cross at exactly one point
- have an (x,y) solution

SOLVING SYSTEMS BY GRAPHING
$\square$

SOLVING SYSTEMS BY GRAPHING
Notes: parallel lines - no solution (NS)

- Same line - infinite solutions (IS)
- graph both lines and see where they cross
- write your final answer as an ordered pair, NS, or IS

4) 

$$
\begin{aligned}
& y=x-4 \\
& y=-\frac{5}{3} x+4
\end{aligned}
$$


5)

$$
\begin{aligned}
& y=x+3 \\
& y=7 x-3
\end{aligned}
$$


4) $y=1 x-4$

$$
\begin{aligned}
& y=\frac{1 x}{1}-4 \\
& y=-\frac{5}{3} x+4
\end{aligned} \quad(3,-1)
$$



5) $y=x+3$
6) $y=\frac{3}{2} x-4$

$$
y=-2 x+3
$$


$(2,-1)$

$$
\text { 8) } \begin{aligned}
& x-4 y=8 \\
& 3 x+4 y=8
\end{aligned}
$$



$(-1,-3)$
9) $4 x-y=-3$
$2 x+y=-3$




Solve each system by substitution.
Notes: get either $x$ or $y$ alone then substitute it into the other equation

- IS - all numbers and variables will cancel out
- NS - all variables will cancel out and 2 different. numbers are left

12) 

$$
\begin{aligned}
& y=-8 x+24 \quad(2,8) \\
& y=6 x-4 \\
& -8 x+24=6 x-4 \\
& -6 x-24-6 x-24 \\
& -14 x=-28 \\
& x=2 \\
& y=6(2)-4 \\
& y=8
\end{aligned}
$$

14) $y=-8 x+3$
15) 

$$
\begin{gathered}
y=-2 x+5 \quad(2,1) \\
y=-5 x+11 \\
-2 x+5=-5 y+11 \\
\frac{1-5 x+5+5 x-5}{3 x=6} \\
x=2 \\
y=-2(2)+5
\end{gathered}
$$

$$
y=1
$$

15) $y=-5 x+18$
16) 

$$
\text { 4) } \begin{aligned}
& y=-8 x+3 \quad(1,-5) \\
& y=-6 x+1 \\
&-8 x+3=-6 x+1 \\
&-8 x-3
\end{aligned}
$$

$$
1-6 x+3+6 x-3
$$

$$
-2 x=-2
$$

$$
x=1
$$

$$
y=-8(1)+3
$$

$$
y=-5
$$

$$
\begin{aligned}
& \text { 16) } \begin{array}{l}
-x-7 y=-20 \\
y=-4 x-1
\end{array} \quad(-1,3) \\
& -x-7(-4 x-1)=-20 \\
& -x+28 x+7=-20 \\
& 27 x=-27 \\
& x=-1 \\
& y=-4(-1)-1 \quad y=3
\end{aligned}
$$

15) 

$$
\begin{gathered}
y=-5 x+18 \quad(5,-7) \\
y=x-12 \\
-5 x+18=x-12 \\
-x-18 \quad-4 x-18 \\
\hline-6 x=-30 \\
x=5 \\
y=-5(5)+18 \\
y=-7
\end{gathered}
$$

17) 

$$
\begin{array}{r}
\text { 7) } \begin{array}{r}
y=-3 x-17 \\
-x-4 y y=-20 \\
-x-4(-3 x-17)=-20 \\
-x+12 x+68=-20 \\
11 x=-88 \\
x=-8 \\
-x+17 \\
y=-3(-8)-17 \\
y=7
\end{array}
\end{array}
$$

$$
\begin{aligned}
& \text { 18) } \begin{array}{l}
y=6 x-8 \\
\text { 18x-3y=24 } \\
\begin{array}{l}
18 x-3(6 x-8) \\
18 x-18 x \\
18 x-24 \\
-24
\end{array}=24
\end{array} \begin{aligned}
24
\end{aligned}
\end{aligned}
$$

Everything cancels!


$$
\text { 19) } \begin{aligned}
2 x-4 y=-18 & (3, \\
y=4 x-6 & \\
2 x-4(4 x-6) & =-18 \\
2 x-16 x+24 & =-18 \\
-24 & -24 \\
\hline-14 x= & -42 \\
x & =3
\end{aligned}
$$

$$
-3-\quad y=4(3)-6
$$

$$
y=6
$$

20) 

$$
\begin{aligned}
& 4 x-y=-20 \\
& x+6 y=20
\end{aligned}
$$

21) 

$$
\begin{aligned}
& x-6 y=7 \\
& -2 x-6 y=4
\end{aligned}
$$

```
20) \(4 x-y=-20\)
    \(x+6 y=20 \times=-6 y+20<(-4,4)\)
    \(4(-6 y+20)-y=-20\)
    \(-24 y+80-y=-20\)
-80
        '- \(25 y=-100\)
        \(y=4\)
    \(x=-6(4)+20\)
    \(x=-4\)
```

    22) \(4 x-y=11\)
    \(-5 x+y=-15\)
    21) $\begin{aligned} & x-6 y=7 \quad x=6 y+7 \\ & -2 x-6 y=4\end{aligned}$ $-2(6 y+7)-6 y=4$
$\begin{array}{r}-12 y-14 \\ +14\end{array}-6 y=4$$\quad(1,-1)$
$-18 y=18$

$$
x=6(-1)+7
$$

$$
x=1
$$

23) $6 x-3 y=24$

$$
3 x+y=7
$$

Solve each system by elimination.
22)

$$
\begin{aligned}
& 4 x-y=11 \\
& -5 x+y=-15 \quad y=5 x-15 \\
& 4 x-1(5 x-15)=11 \\
& \begin{array}{l}
4 x-5 x+15=11 \\
-x=-4 \\
-15-15
\end{array} \quad(4,5) \\
& x=4 \\
& y=5(4)-15 \\
& y=5
\end{aligned}
$$

Solve each system by elimination.
Notes:
Notes:

$$
\text { 23) } \begin{gathered}
6 x-3 y=24 \\
3 x+y=7 \quad y=-3 x+7 \\
6 x-3(-3 x+7)=24 \\
\begin{array}{c}
6 x+9 x \\
\hline 621 \\
15 x \\
=21 \\
x
\end{array}=35 \\
\qquad-21 \\
y=-3(3)+7 \\
y=-2
\end{gathered}
$$

24) $8 x-5 y=17$
25) $-2 x+7 y=1$

Solve each system by elimination.
Notes: get rid of $x$ or $y$

- have to get opposite \#'s

$$
(e x \cdot 3 \&-3)
$$

- Can get IS or NS as an answer

24) 

$$
\begin{gathered}
8 x-5 y=17 \\
-8 x+5 y=-21 \\
0=-4 \\
\text { NS }
\end{gathered}
$$

25) 

$$
\begin{gathered}
-2 x+7 y=1 \\
2 x+9 y=15 \\
\hline 16 y=16 \\
y=1 \\
2 x+9(1)=15 \\
2 x+9=15 \\
2 x=6 \\
x=3
\end{gathered}
$$

26) $x+10 y=26$
27) $-4 x+8 y=28$
$\square$
28) 

$$
\begin{aligned}
& x+10 y=26 \\
& -6 x-10 y=-6 \\
& -5 x=20 \\
& x=-4 \\
& -4+10 y=26 \\
& 10 y=30 \\
& y=3
\end{aligned}
$$

27) 

$$
\begin{gathered}
-4 x+8 y=28 \\
4 x-y=14 \\
7 y=42 \\
y=6 \quad(5,6) \\
4 x-6=14 \\
4 x=20 \\
x=5
\end{gathered}
$$

-4-
28)

$$
\begin{aligned}
& 2 x-8 y=-4 \\
& x-8 y=6
\end{aligned}
$$

29) 

$$
\begin{aligned}
& 8 x+3 y=20 \\
& 4 x+3 y=4
\end{aligned}
$$

```
28) \(2 x-8 y=-4\)
\[
\frac{-x+8 y=-6}{x=-10} \quad(-10,-2)
\]
\[
\begin{aligned}
& 2(-10)-8 y=-4 \\
& -20-8 y=-4 \\
& +20 \quad+20
\end{aligned}
\]
\[
-8 y=16
\]
\[
y=-2
\]
\[
\text { 30) }-5 x-6 y=1
\]
\[
-5 x-y=21
\]
```

32) $3 x-5 y=-21$
33) $8 x+3 y=20$

$$
\begin{gathered}
-4 x+3 y=-4 \\
\hline 4 x=16 \\
x=4
\end{gathered}
$$

$$
8(4)+3 y=20
$$

$$
\begin{aligned}
32+3 y & =20 \\
-32 & =-\frac{12}{3}
\end{aligned}
$$

$$
y=-4
$$

31) $-2 x+2 y=-12$
$-2 x+2 y=-12$
32) $8 x-2 y=18$

$$
\text { 30) } \begin{gathered}
-5 x-6 y=1 \\
+5 x+y=21 \\
\hline-5 y=-20 \quad(-5,4) \\
y=4 \\
-5 x-6(4)=1 \\
-5 x-24=1 \\
-5 x=25 \\
x=-5
\end{gathered}
$$

31) $-2 x+2 y=-12$
$+2 x+12 y=-12$
Everything carcels! $\}=5$
32) $3 x-5 y=-21$
$-6 x-6 y=-6$
33) $8 x-2 y=18$
$-4 x-y=-7$
34) $12 x+3 y=-27$
$6 x+y=-13$
35) $12 x+3 y=24$
$3 x-y=13$
$\square$
36) 

$3 x-5 y-21$
$-6 x-6 y=-6$$\quad(-2,3)$

$$
-16 y=-48
$$

$1 \quad y=3$
$-6 x-6(3)=-6$
$-6 x-18=-6$

$$
\begin{aligned}
& 18+18 \\
& +18 \\
& \hline
\end{aligned}
$$

$-6 x=12 \quad x=-2$
34) $12 x+3 y=-27$
$6 x+y=-13$

$$
\begin{aligned}
& \text { 33) } 8 x-2 y=18 \\
& 2(-4 x-y=-7) \\
& \frac{-8 x-2 y}{-8 y}=-14 \\
& -4 y=4 \\
& y=-1 \\
& 8 x-2(-1)=18 \\
& 8 x+2=18 \\
& 8 x=16 \quad x=2
\end{aligned}
$$

35) $12 x+3 y=24$
$3 x-y=13$
36) $-90 x+10 y=-23$

514 6.1-17
37) $5 x+5 y=-25$

1~1 8 ., - 9
$\square$
34) $12 x+3 y=-27$

$$
-2(6 x+y=-13)
$$

$$
(-2,-1)
$$

$$
12 x+3(-1)=-27
$$

$$
12 x-3=-27
$$

$$
12 x=-24
$$

$$
x=-2
$$

36) $-90 x+10 y=-23$ $54 x-6 y=12$
37) 

$$
\begin{aligned}
& 5 x+5 y=-25 \\
& -4 x+8 y=-28
\end{aligned}
$$

$$
\begin{aligned}
& \text { 35) } 12 x+3 y=24 \\
& -4(3 x-y=13) \\
& \begin{aligned}
-12 x+4 y & =-52 \\
7 y & =-28
\end{aligned}(3,-4)
\end{aligned}
$$



J une 18 2015.GWB - 19/22 - Thu J un 182015 10:25:15


The senior classes at High School A and High School B planned separate trips to the indoor climbing gym. The senior class at High School A rented and filled 3 vans and 13 buses with 612 students. High School B rented and filled 3 vans and 6 buses with 297 students. Each van and each bus carried the same number of students. Find the number of students in each van and in each bus.

$$
\begin{gathered}
\left.A \cdot \begin{array}{rl}
3 v+13 b & =612 \\
B-3 v+6 b & =-297 \\
7 b & =315 \\
b & =45 \\
3 v+13(45)=612 \\
3 v+585 & =612
\end{array}\right)=92=9
\end{gathered}
$$



The school that Arjun goes to is selling tickets to the annual talent show. On the first day of ticket sales the school sold 8 senior citizen tickets and 2 child tickets for a total of $\$ 62$. The school took in $\$ 80$ on the second day by selling 8 senior citizen tickets and 8 child tickets. Find the price of a senior citizen ticket and the price of a child ticket.

senior citizen ticket: \$7, child ticket: \$3 cherry pie: S12, pumpkin pie: $\$ 16$
42) daylily: S10, pot of ivy: S8
44) hosta: S2, geranium: S9 rose bush: S4, bunch of ormamental grass: S2
bag of windflower bulbs: S4, package of crocus bulbs: S15 fte of grass sod: : 7 , potofiry: 59

