

Benchmark 2--Study Guide

Solve each equation.

$$1) -3k - 4 = -8 - 5k$$

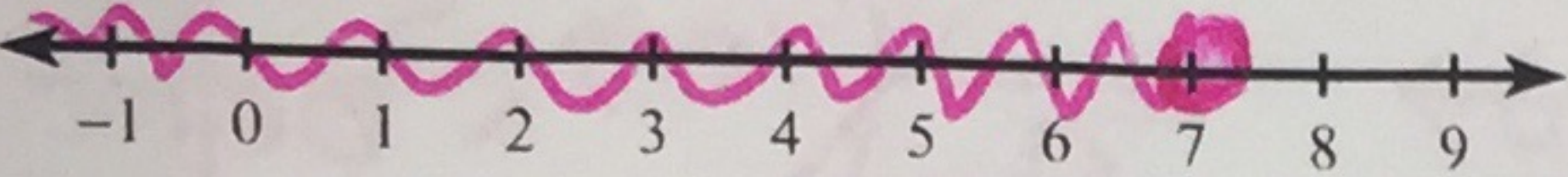
$$\begin{array}{r} +5k \quad +4 \quad +4 \quad +5k \\ \hline 2k = -4 \\ k = -2 \checkmark \end{array}$$

$$2) 6 - 7x = -1 - 7x$$

$$\begin{array}{r} +7x \quad +7x \\ \hline 6 = -1 \end{array}$$

No Solution
b = -1 x
Not true

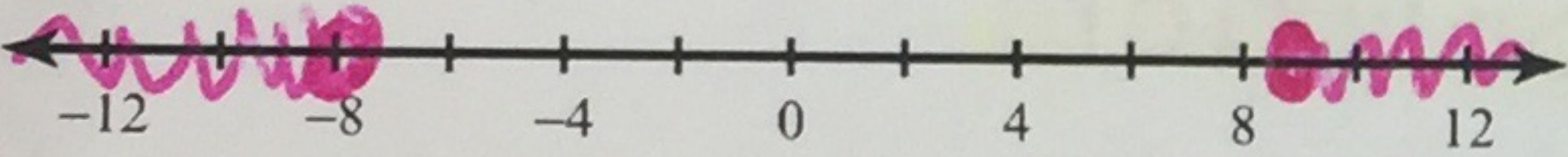
Solve each inequality and graph its solution.

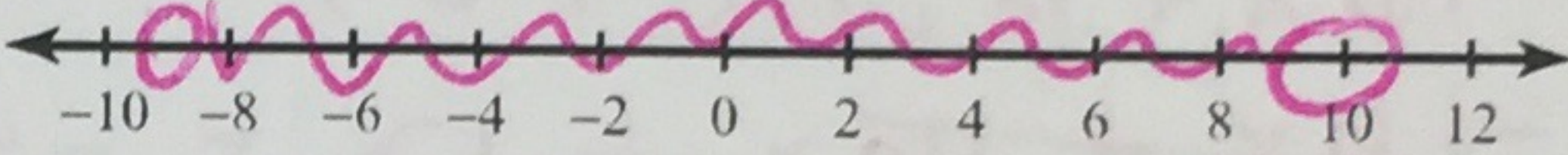
$$3) -106 \leq -3(5x + 5) + 2x$$


$$\begin{array}{r} -106 \leq -3(5x + 5) + 2x \\ -106 \leq -15x - 15 + 2x \\ -106 \leq -13x - 15 \\ +15 \quad +15 \\ \hline -91 \leq -13x \\ \frac{-91}{-13} \leq \frac{-13x}{-13} \\ 7 \geq x \end{array}$$

Remember to Flip inequality Symbol when you divide by a negative

Solve each compound inequality and graph its solution.

$$4) -6 + 3b \geq 21 \text{ or } 9 + 7b \leq -47$$


$$5) 6m + 5 > -49 \text{ and } -7m - 3 > -73$$


$$\begin{array}{r} -6 + 3b \geq 21 \\ +6 \quad +6 \\ \hline 3b \geq 27 \\ b \geq 9 \end{array} \quad \begin{array}{r} 9 + 7b \leq -47 \\ -9 \quad -9 \\ \hline 7b \leq -56 \\ b \leq -8 \end{array}$$

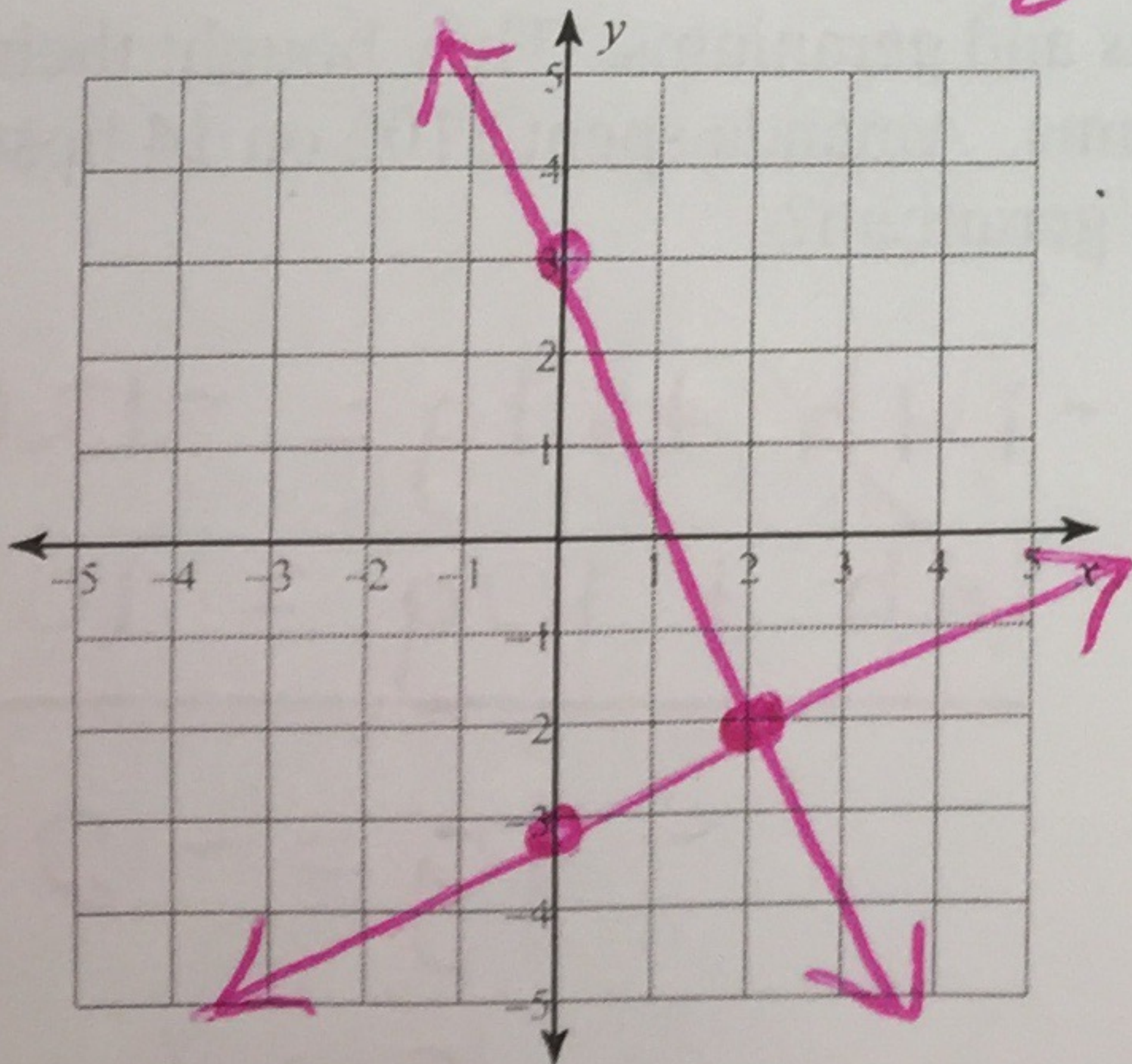
$b \geq 9$ or $b \leq -8$

$$\begin{array}{r} 6m + 5 > -49 \\ -5 \quad -5 \\ \hline 6m > -54 \\ m > -9 \end{array} \quad \begin{array}{r} -7m - 3 > -73 \\ +3 \quad +3 \\ \hline -7m > -70 \\ \frac{-7m}{-7} > \frac{-70}{-7} \\ m < 10 \end{array}$$

Solve each system by graphing.

$$6) 2y = -5x + 6 \rightarrow y = -\frac{5}{2}x + 3$$

$$-3 + \frac{1}{2}x = y \rightarrow y = \frac{1}{2}x - 3$$

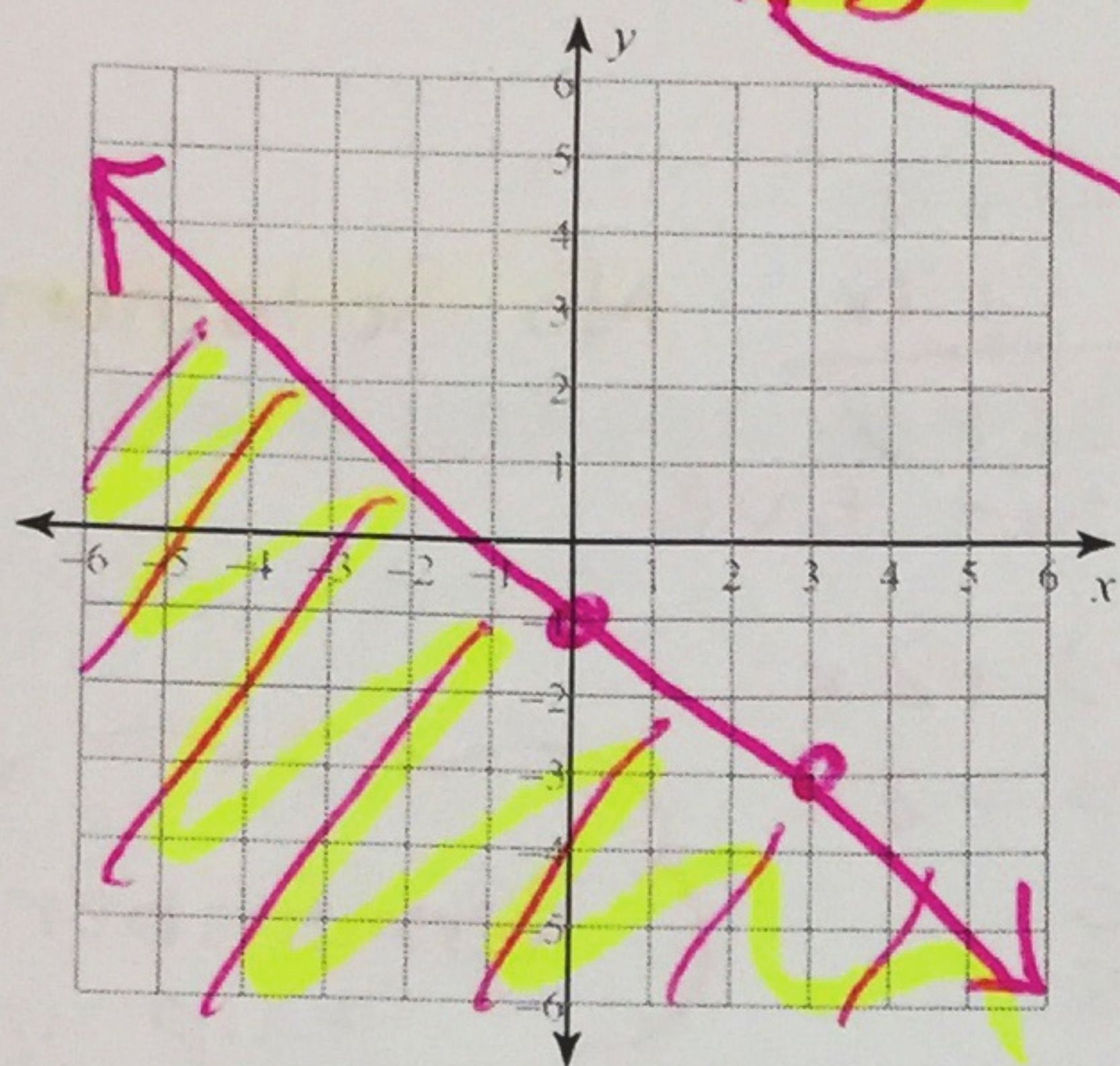


Solution = (2, -2)

Sketch the graph of each linear inequality.

7) $2x + 3y \leq -3$

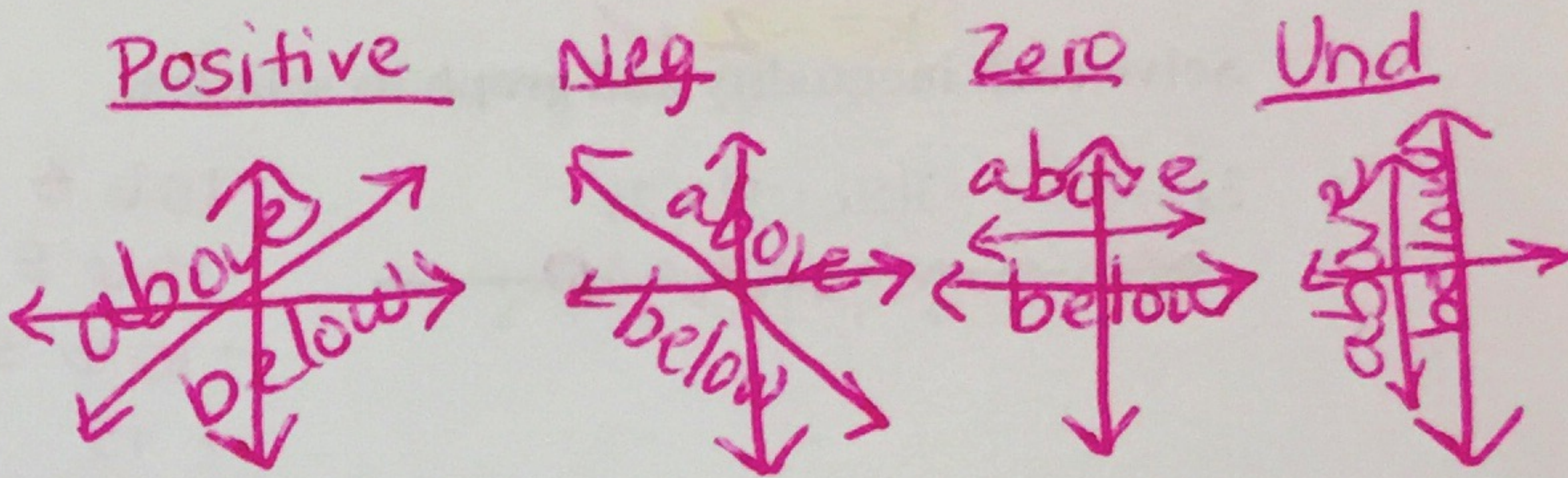
$y \leq -\frac{2}{3}x - 1$



solid below

Shade
above $>, \geq$
below $<, \leq$

line
dotted (dashed) $>, <$
solid \geq, \leq



Solve each system by substitution.

8) $-8x + y = -6 \rightarrow y = 8x + 6$
 $-16x + 2y = -4$

$-16x + 2(8x + 6) = -4$
 $-16x + 16x + 12 = -4$

No Solution

$12 = -4$ Not true

Solve each system by elimination.

9) $\begin{cases} 2x + 4y = 14 \\ 9x + 8y = -7 \end{cases} \rightarrow \begin{cases} -4x - 8y = -28 \\ 9x + 8y = -7 \end{cases}$
 $\underline{\hspace{1.5cm}}$
 $5x = -35$
 $x = -7$

$2(-7) + 4y = 14$
 $-14 + 4y = 14$
 $\underline{\hspace{1.5cm}}$
 $4y = 28$
 $y = 7$

$(-7, 7)$

10) Jaidee and Amanda each improved their yards by planting hostas and geraniums. They bought their supplies from the same store. Jaidee spent \$63 on 7 hostas and 7 geraniums. Amanda spent \$102 on 14 hostas and 10 geraniums. What is the cost of one hosta and the cost of one geranium?

$-2(7h + 7g = 63) \rightarrow -14h - 14g = -126$
 $14h + 10g = 102$
 $\underline{\hspace{1.5cm}}$
 $-4g = -24$
 $g = 6$

geranium - \$6

hosta - \$3

$7h + 7(6) = 63$
 $7h + 42 = 63$
 $7h = 21$
 $h = 3$

- 11) A rectangle has a length of $x - 3$ inches and a width of 6 inches. For what values of x is the area of the rectangle greater than the perimeter of the rectangle? Draw a diagram to help.

$$\text{area} = l \times w$$

$$\text{Perimeter} = 2l + 2w$$

$$6(x-3) > 2(x-3) + 2(6)$$

$$6x - 18 > 2x - 6 + 12$$

$$6x - 18 > 2x + 6$$

$$4x > 24$$

$$x > 6$$

- 12) A cyclist 45 miles in 4 hours. What is her speed in feet per second?

$$\frac{45 \text{ miles}}{4 \text{ hours}} = \frac{237600 \text{ ft}}{14400} = 16.5$$

5280 ft
in a mile

- 13) Solve $\frac{m}{x} = k - 6$ for m .

3600 sec in
a minute

$$x \cdot \frac{m}{x} = (k-6) \cdot x$$

$$m = x(k-6) \text{ or } m = xk - 6x$$

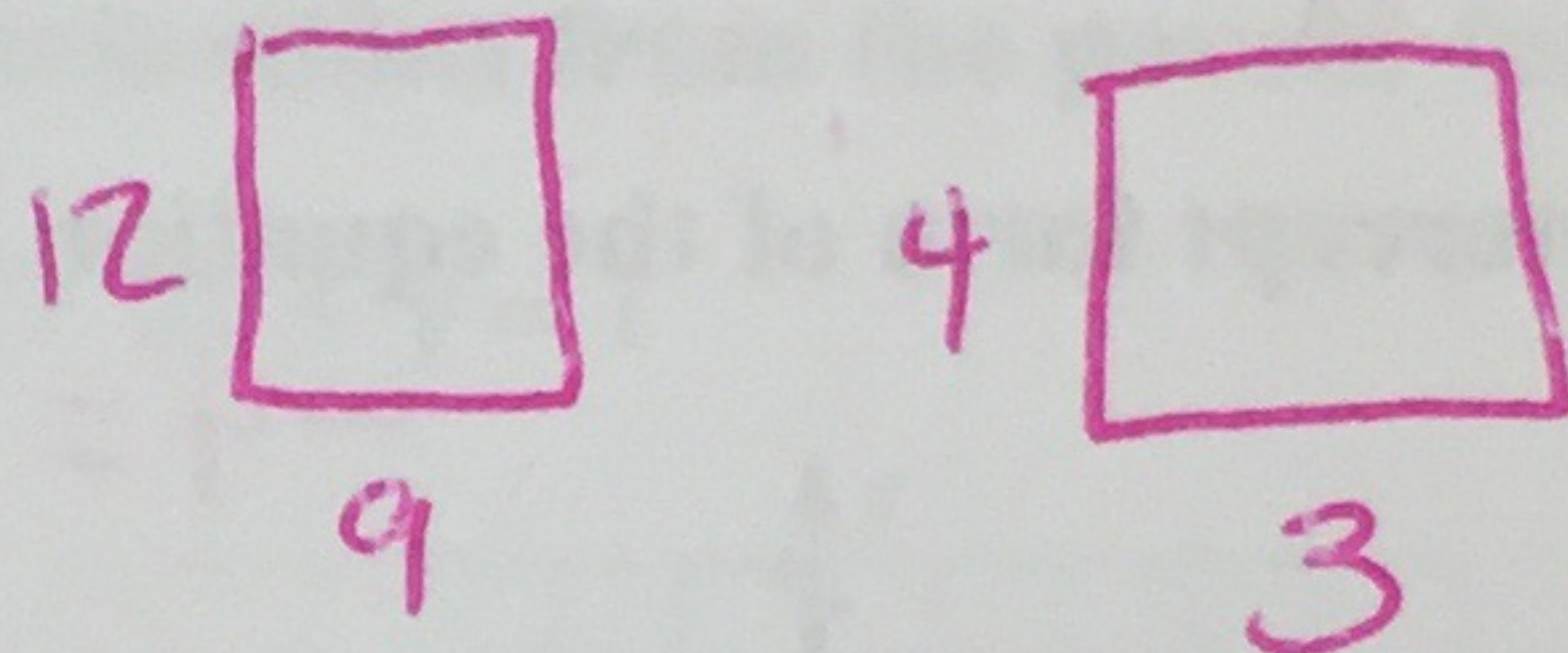
- Remember x has to multiply to both

- 14) A rectangle has side lengths of 12 inches and 9

inches. Every dimension is multiplied by $\frac{1}{3}$ to

form a new rectangle.

What is the scale factor? $\frac{1}{3}$



What is the ratio of the corresponding sides of the first figure to the second figure? $3:1$ or 3

What is the ratio of the perimeters? $3:1$ or 3 $[42:14] P$

What is the ratio of the areas? $9:1$ or 9 $[108:12] A$

- 15) An architect built a scale model of a shopping mall. On the model, a circular fountain is 20 inches tall and 22.5 inches in diameter. The actual fountain is to be 8 feet tall. What will be the diameter of the fountain?

$$\frac{20}{22.5} = \frac{8}{x}$$

(You don't
have to
convert)

$$x = 9$$

Solve each proportion.

$$16) \frac{9}{7} = \frac{r+6}{10}$$

$$9(10) = 7(r+6)$$

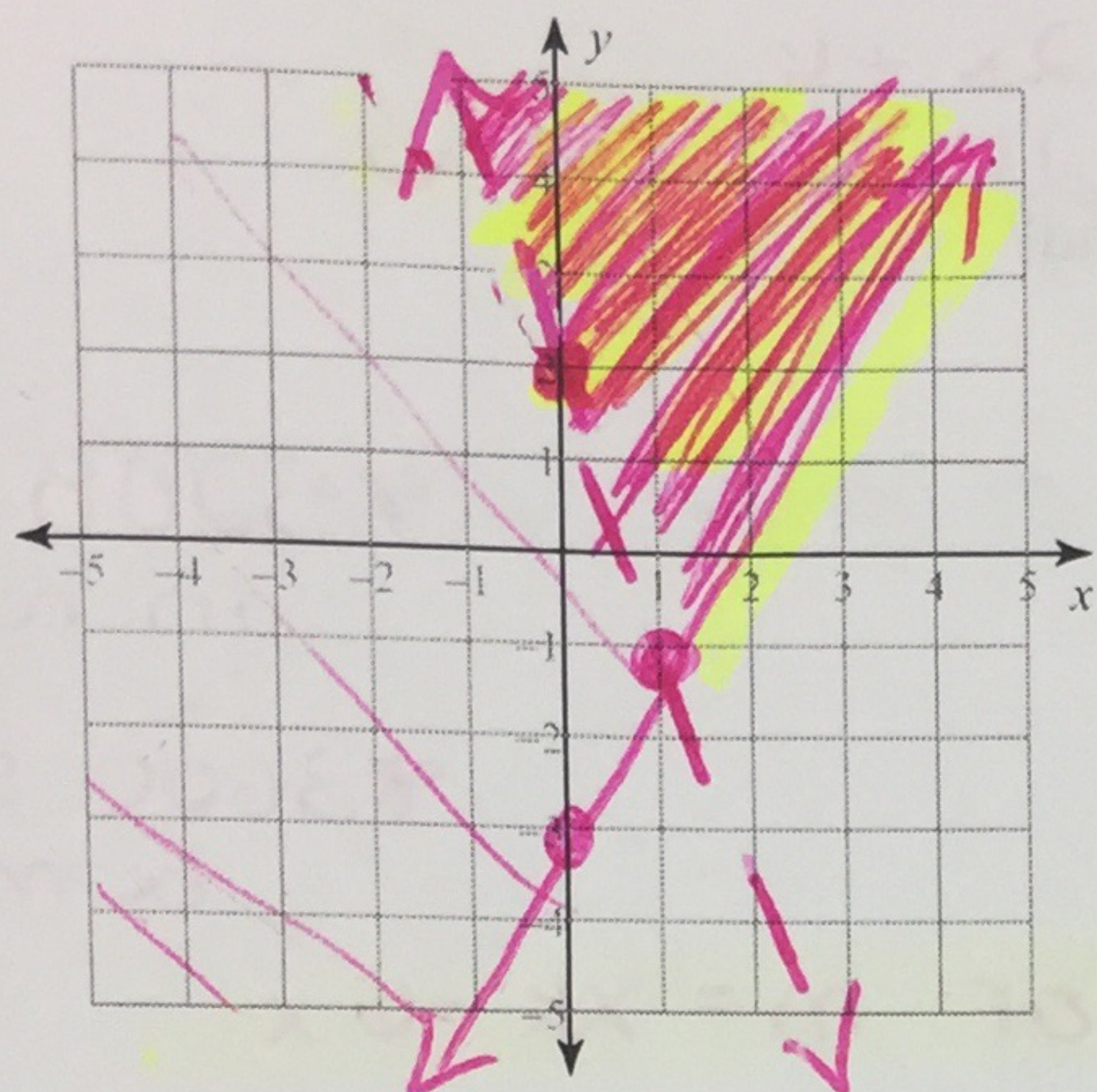
$$90 = 7r + 42$$

$$48 = 7r$$

$$6.86 = r$$

Sketch the solution to each system of inequalities.

17) $y \geq 2x - 3$ solid above
 $y > -3x + 2$ dotted above



Write the slope-intercept form of the equation of each line given the slope and y-intercept.

18) Slope = -1 , y-intercept = 3
 m b

$y = -1x + 3$ or $y = -x + 3$

Write the slope-intercept form of the equation of the line through the given point with the given slope.

19) through: $(3, -4)$, slope = $-\frac{7}{3}$
 x y m

$-4 = -\frac{7}{3}(3) + b$
 $-4 = -7 + b$
 $3 = b$

$y = -\frac{7}{3}x + 3$

Write the slope-intercept form of the equation of the line through the given points.

20) through: $(0, 3)$ and $(4, -2)$
 x y y int

slope: $\frac{3 - (-2)}{0 - 4} = \frac{5}{-4}$

$y = -\frac{5}{4}x + 3$

Write the slope-intercept form of the equation of the line described.

21) through: $(-4, -1)$, parallel to $y = \frac{3}{2}x + 1$
 x y m

Parallel = same slope

$-1 = \frac{3}{2}(-4) + b$

$-1 = -6 + b$

$5 = b$

$y = \frac{3}{2}x + 5$

22) through: $(1, -2)$, perp. to $y = 3$

x value

$x = 1$

perp to $y = 3$ is $x =$